

Realization of Chart Datum and Its Connection to the Mainland Height System

Cornelis Slobbe

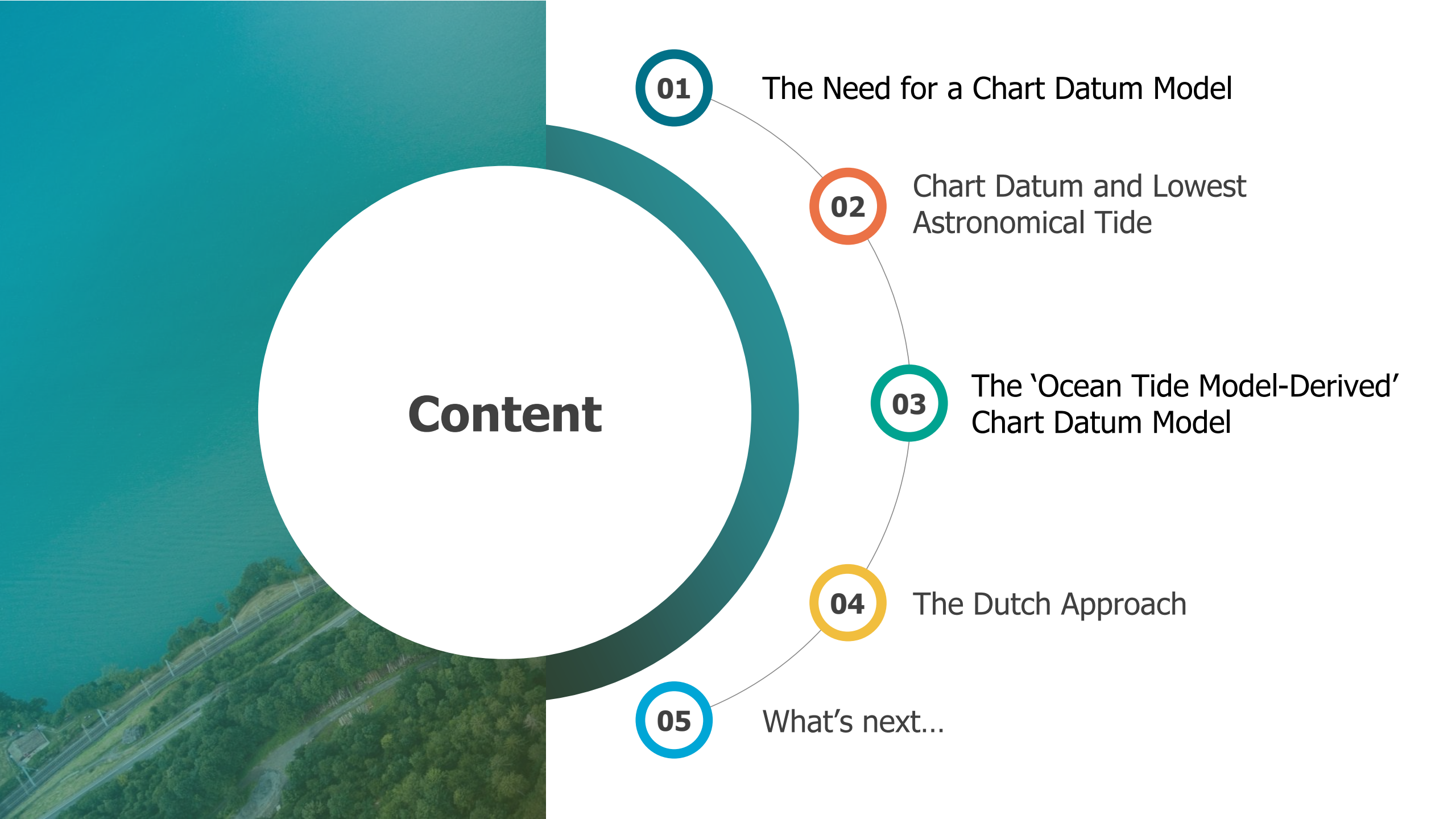




This is an *interdisciplinary* exercise and not just about linking reference surfaces...

...It's about bringing together different professional worlds / disciplines, each holding a part of the solution!

Content



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graph TD; 01((01)) --- 02((02)); 02 --- 03((03)); 03 --- 04((04)); 04 --- 05((05)); 05 --- 01
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01

The Need for a Chart Datum Model

02

Chart Datum and Lowest
Astronomical Tide

03

The 'Ocean Tide Model-Derived'
Chart Datum Model

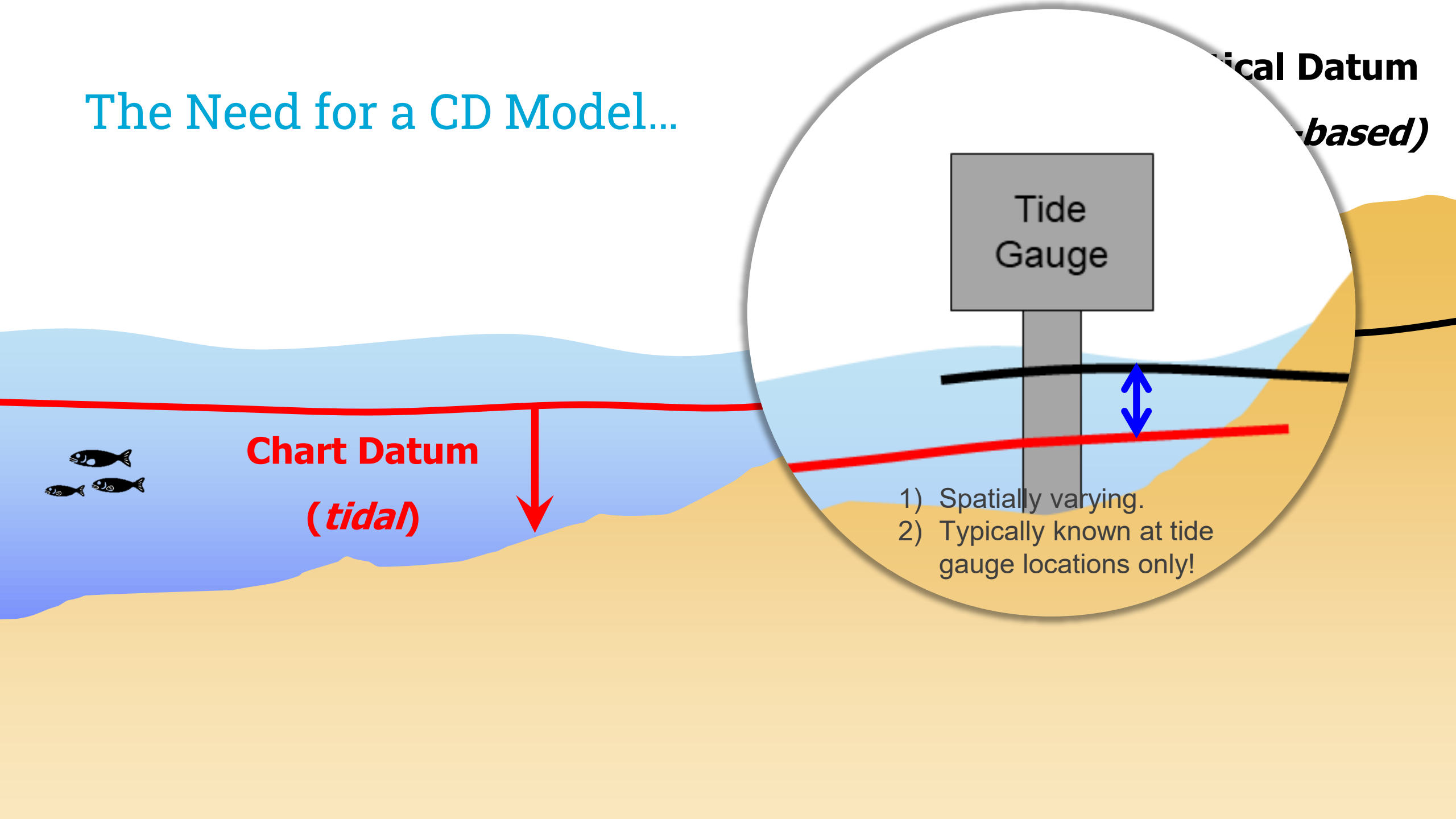
04

The Dutch Approach

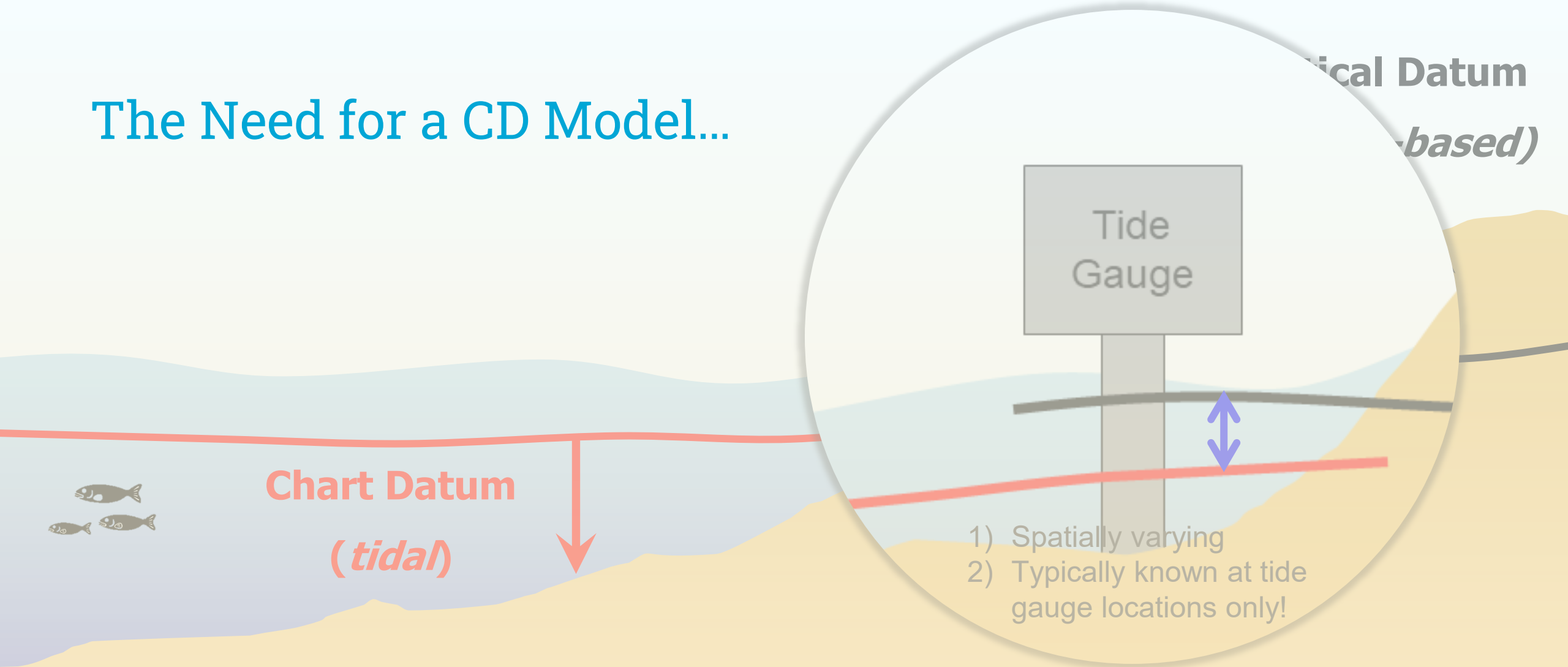
05

What's next...

The Need for a CD Model...

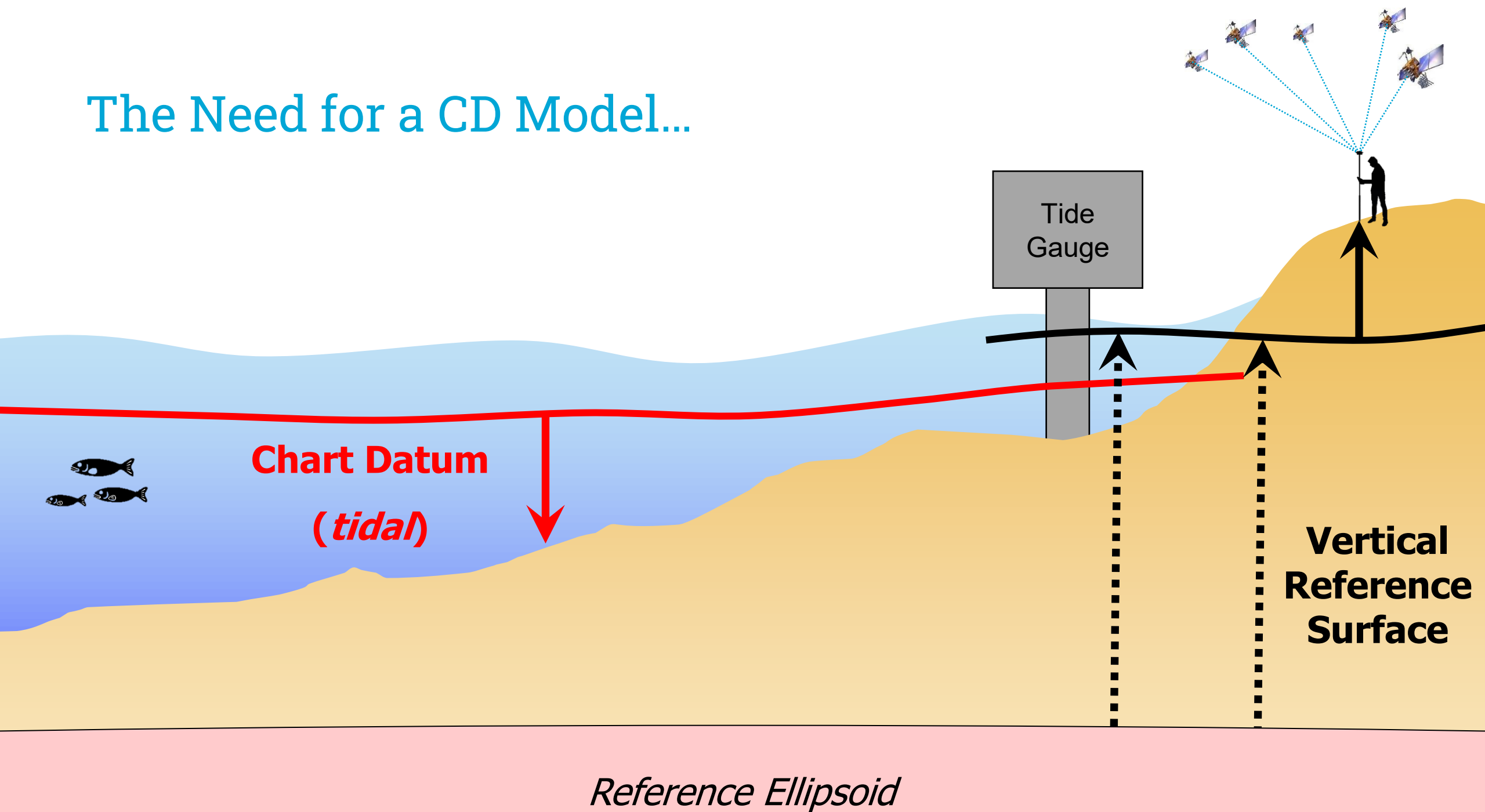


The Need for a CD Model...

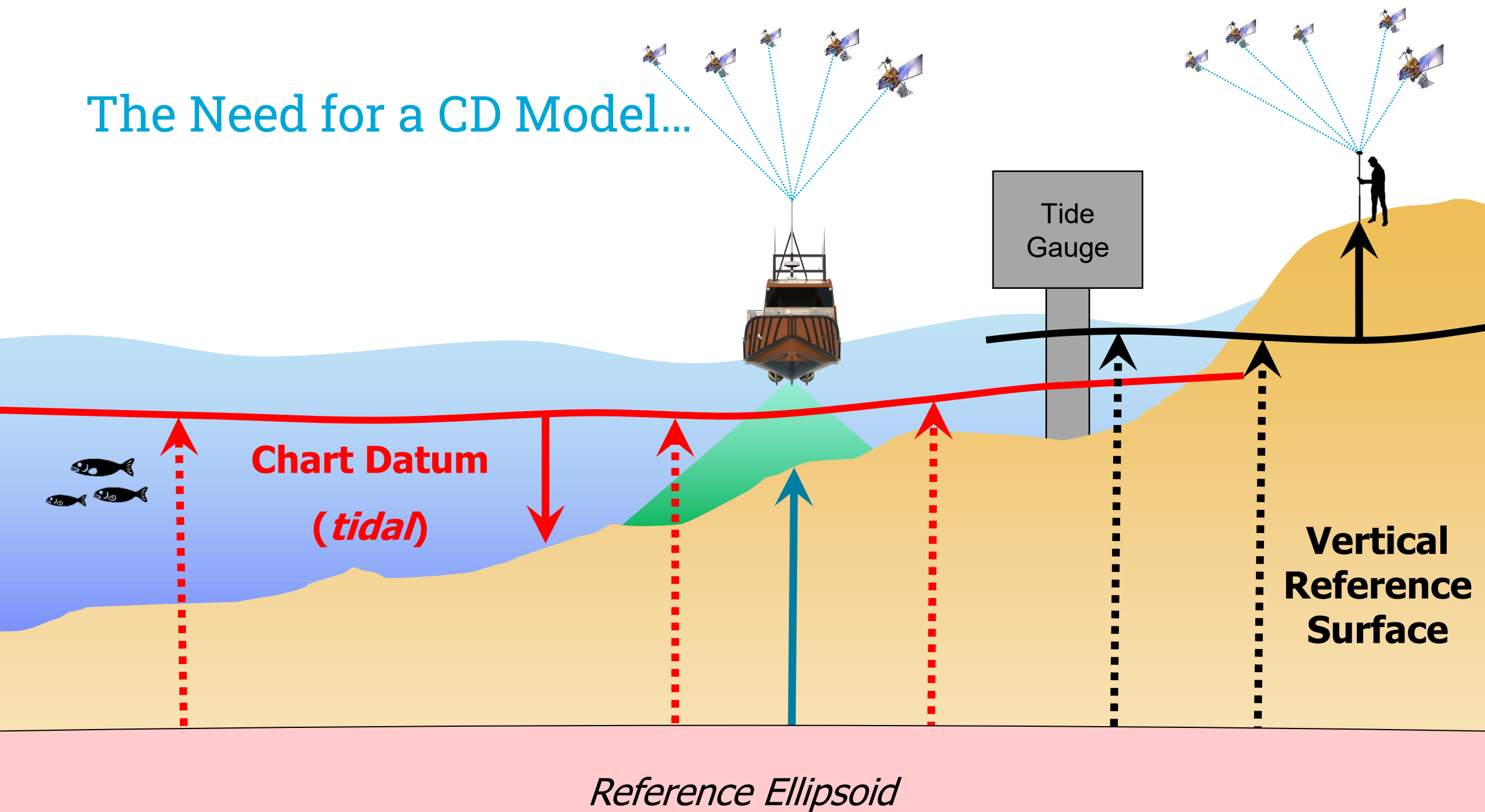


To enable the *integration* of land and sea datasets, both reference surfaces need to be described in 3D space.

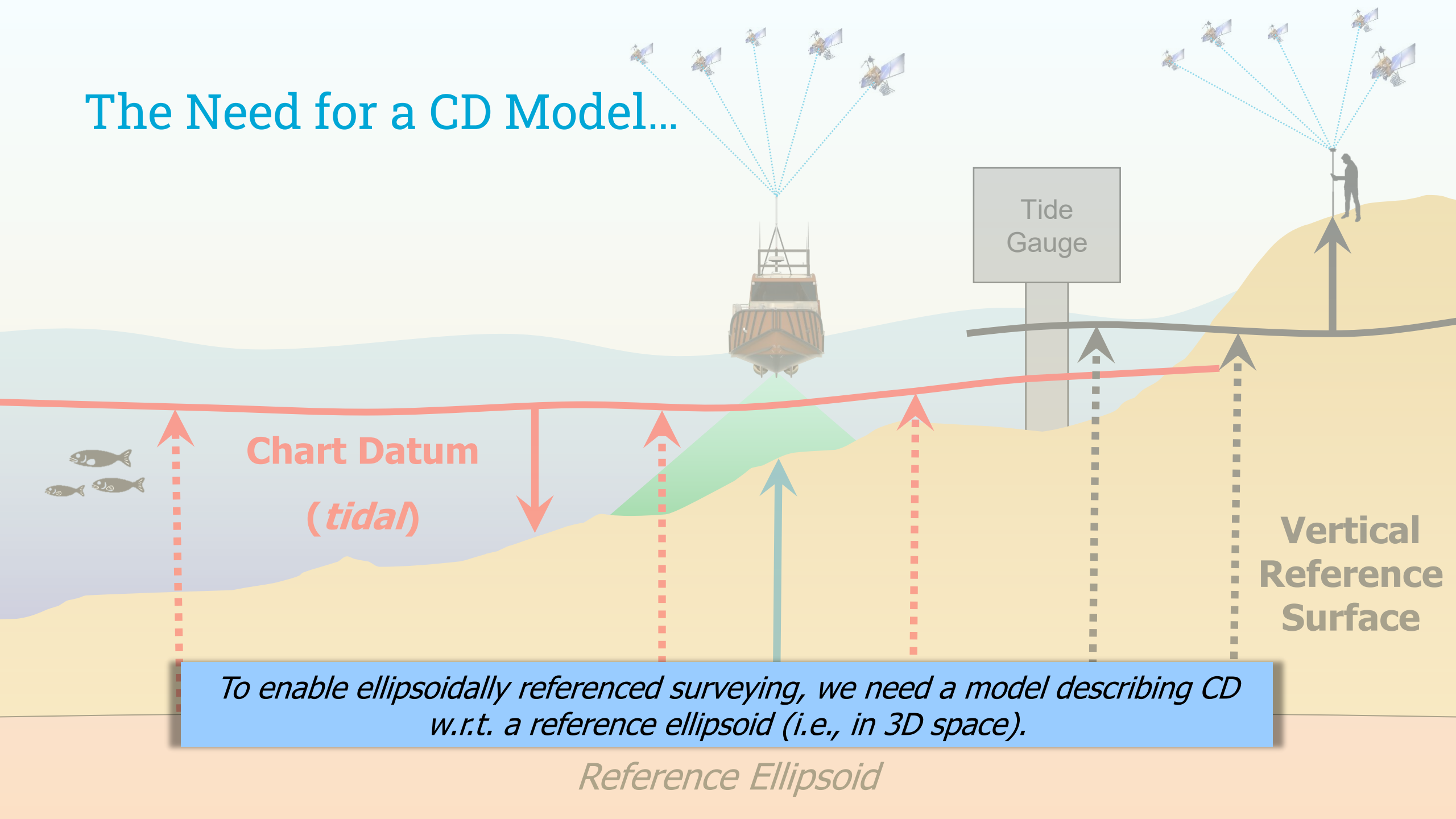
The Need for a CD Model...



The Need for a CD Model...



The Need for a CD Model...



To enable ellipsoidally referenced surveying, we need a model describing CD w.r.t. a reference ellipsoid (i.e., in 3D space).

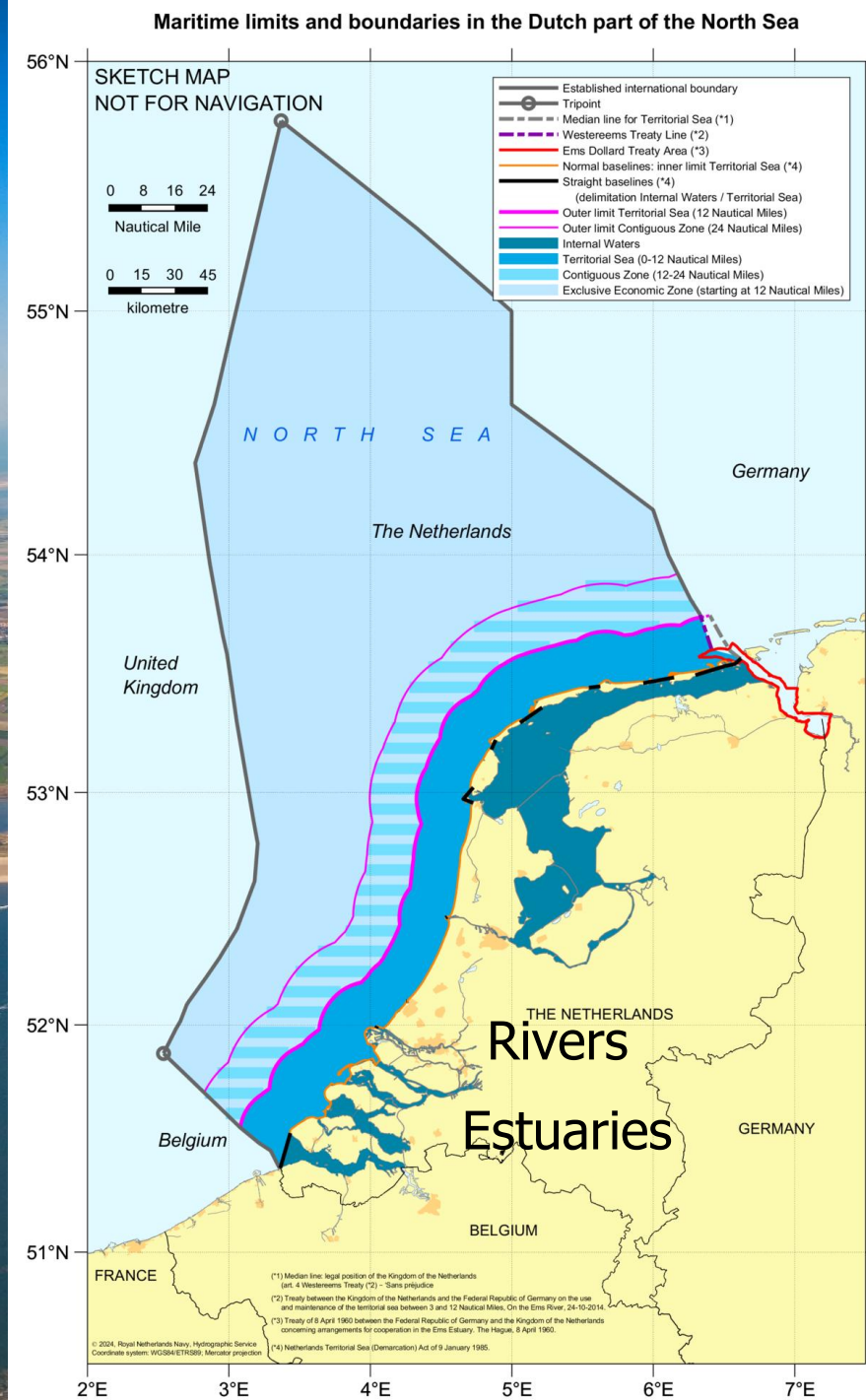
Reference Ellipsoid

The CD Model Needs to Cover...

Exclusive Economic Zone

Coastal Waters

Inland Seas

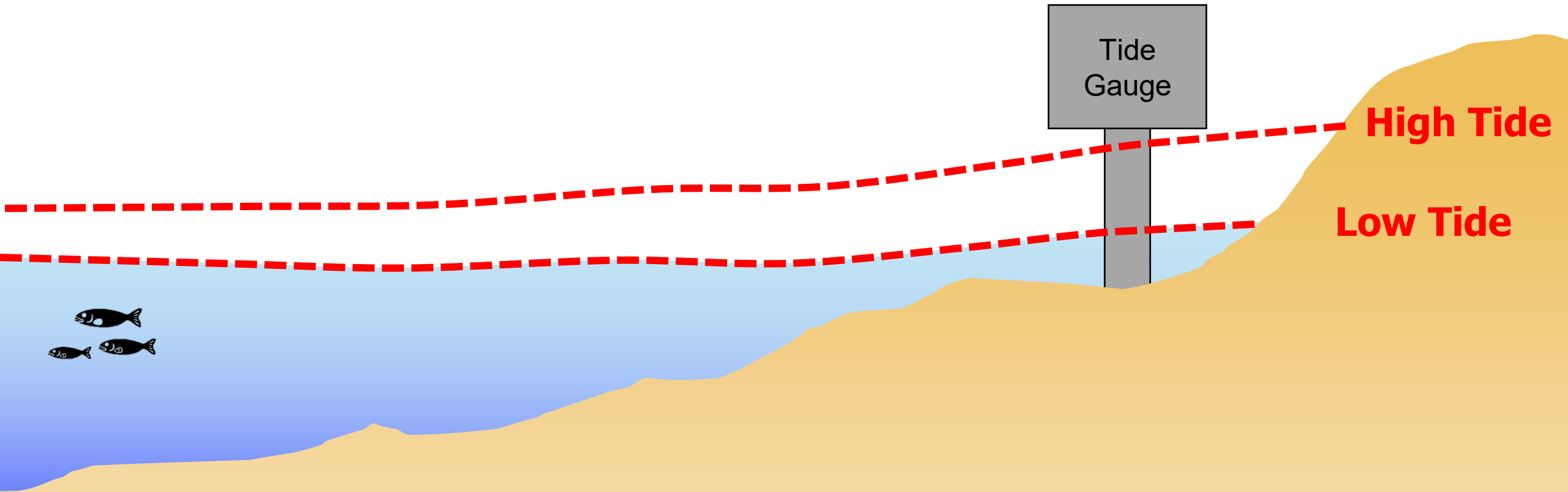


The Question...

*How to obtain ellipsoidal
heights of Chart Datum?*



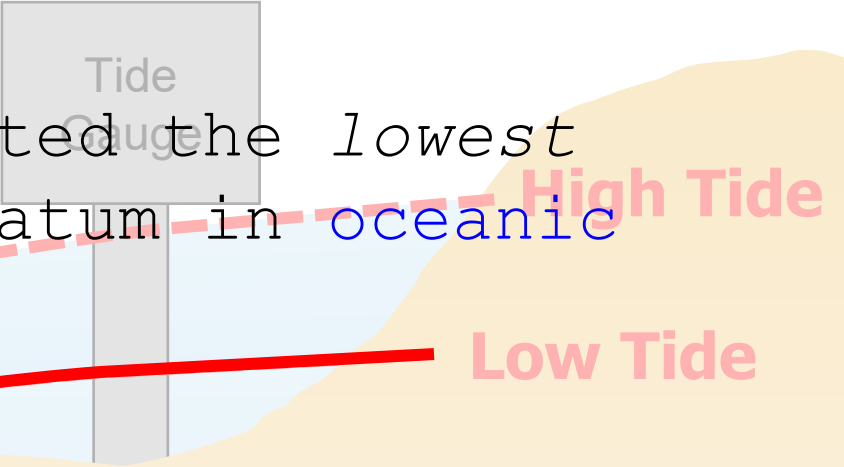
Tidal Datums



*A tidal datum is a standard elevation defined by
a **certain phase of the tide** (NOAA, 2025).*

Chart Datum

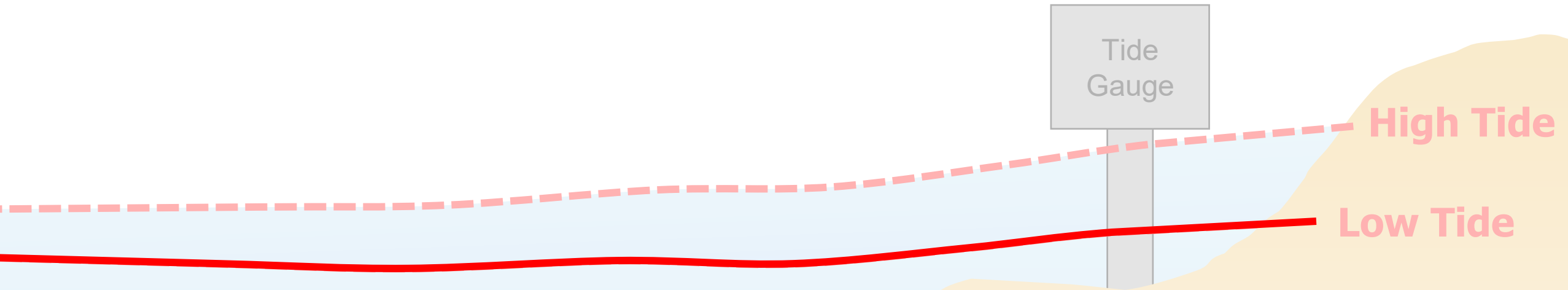
To support safe navigation, the IHO adopted the *lowest* astronomical tide (LAT) level as chart datum in *oceanic* tidal areas^{*1} (IHO Resolution 3/1919)...

A diagram illustrating the concept of Chart Datum. It shows a grey tide gauge labeled 'Tide Gauge' on a sandy beach. A dashed red line represents the 'High Tide' level, and a solid red line represents the 'Low Tide' level. The ocean is depicted in light blue, and the beach in light yellow.

 LAT $\equiv$ lowest tide level which can be predicted to occur under *average* meteorological conditions and under any combination of astronomical conditions

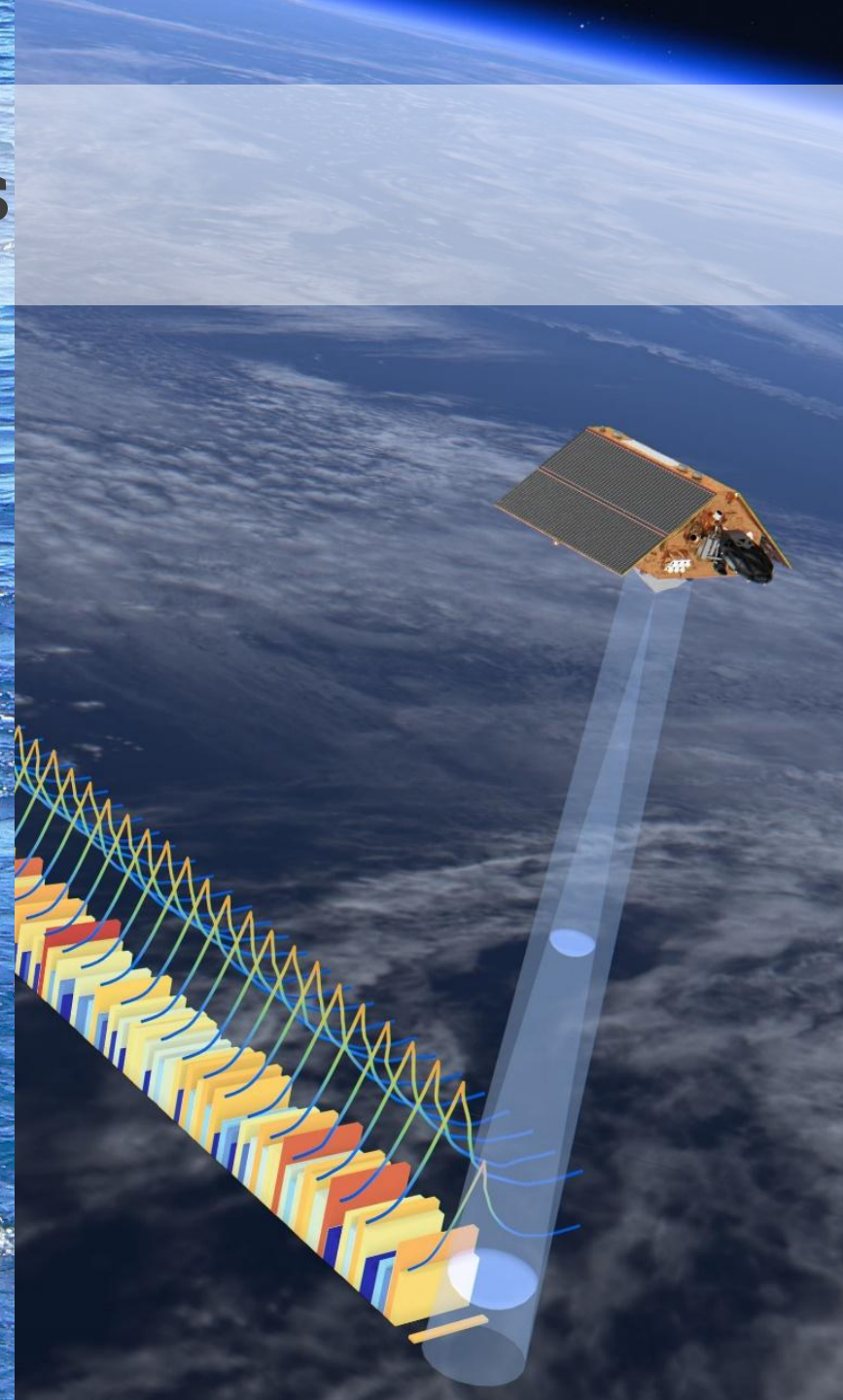
^{*1} not in mixed/inland/non-tidal waters

IHO's Recommendation...



"It is recommended that LAT and HAT be calculated either over a minimum period of 19 years using harmonic constants derived from a minimum of one year's observations or by other proven methods known to give reliable results. Tide levels should, if possible, reflect the estimated uncertainty values obtained during the determination of these levels."

Needed: Observed Water Level Records



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Temporal Resolution:

High (5–10 minutes)

Low (~10 days)

Spatial Coverage:

Poor (mostly coastal areas)

Good (global coverage, except near poles & in coastal waters)

Data Availability:

Often restricted; not always publicly available

Freely and publicly available (since 1992)

Continuity & Homogeneity of Records:

Often discontinuous and inhomogeneous over long periods

Continuous and homogeneous long-term record (since 1992)

Reference Frame:

May use local datum; not necessarily referenced to ellipsoid

Referenced to ellipsoid

Impact of Vertical Land Motion:

Affected (unless corrected using GNSS)

Not affected

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Tide gauges offer high temporal resolution and 'coverage' in coastal regions, while satellite radar altimetry provides broad spatial coverage over open oceans.

→ Both are essential!

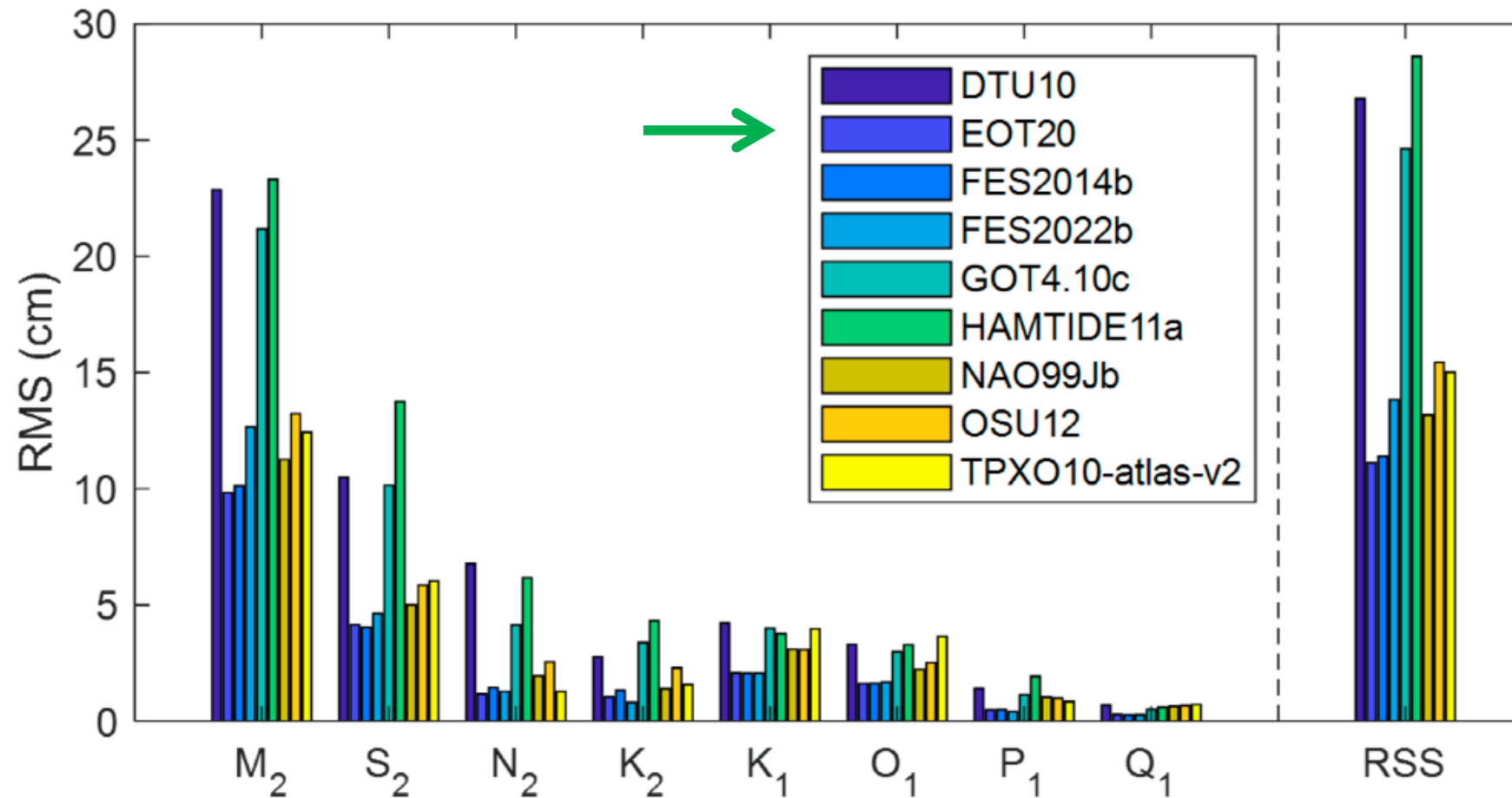
The 'Ocean Tide Model-Derived' CD Model

- **Strategy:** Combine CD estimates from [altimeter-derived tidal atlases](#) (i.e., empirical ocean tide models) & mean sea surface (MSS) models with estimates derived from tide gauge records.
 - **Available models:** DTU23 Global Ocean Tide model (DTU Space), EOT20 (DGFI-TUM), GOT5.6 (Goddard Space Flight Center).
 - **Key differences** between models:
 - Estimation procedure (*e.g., response method vs. harmonic analysis*).
 - Data used (*e.g., missions, time span, data above 66° latitude*).
 - Spatial resolution ($1/8^\circ - 1/16^\circ$).
 - The constituents being estimated / inferred.
 - Treatment of self-attraction and loading (*in EOT/GOT, loading tides are separated from ocean tides*).
- **No single model performs best in all regions!**

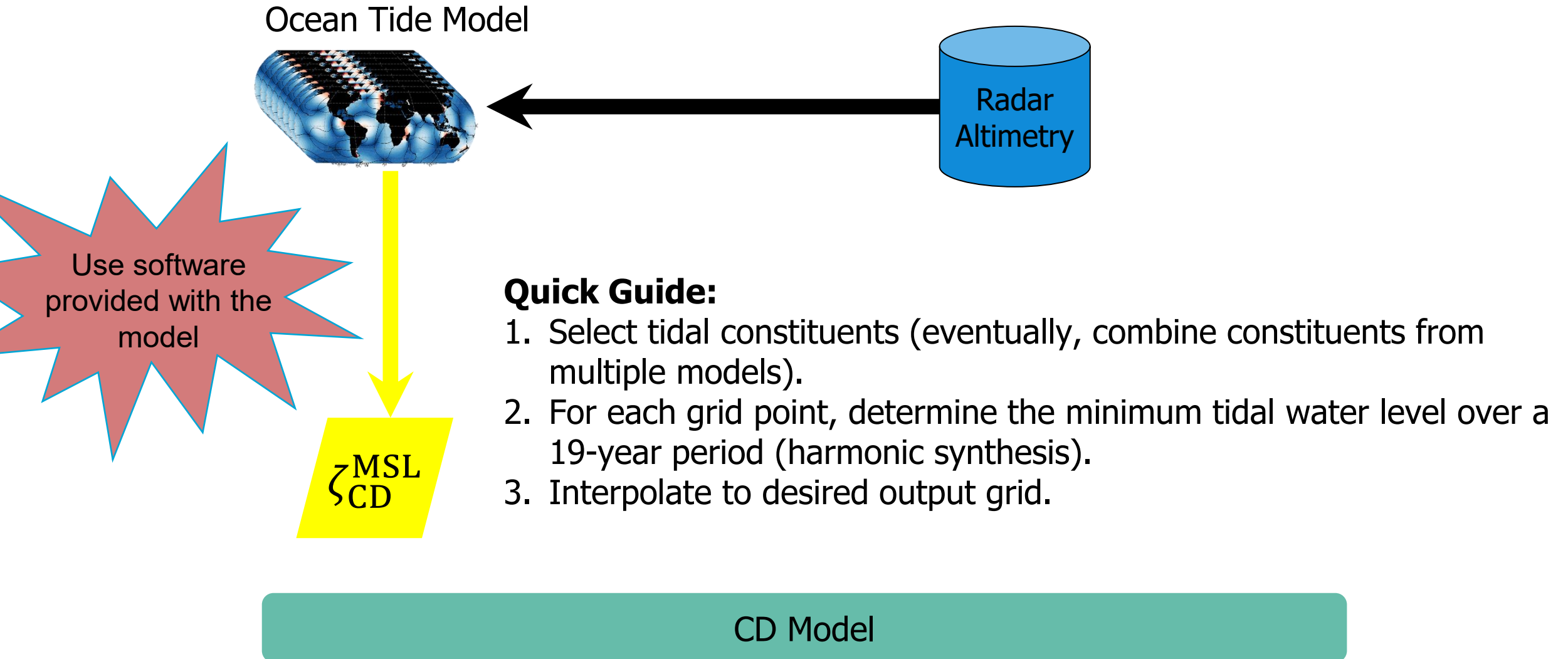
Alternative: Use Assimilative Ocean Tide Model

- **Assimilative** Ocean Tide Models combine **numerical modeling** with data assimilation.
 - **Available models:** FES2022b (CNES), TPXO10 (OSU).
 - **Key differences** compared to empirical ocean tide models:
 - Tide gauge-derived tides already incorporated (*FES: limited to a set of 295 tide gauges*).
 - Provided at higher spatial resolution (*1/30° degrees*).
 - More tidal constituents included (*34 for FES2022b; not all improved by data assimilation*).
- **The accuracy is not necessarily better!**

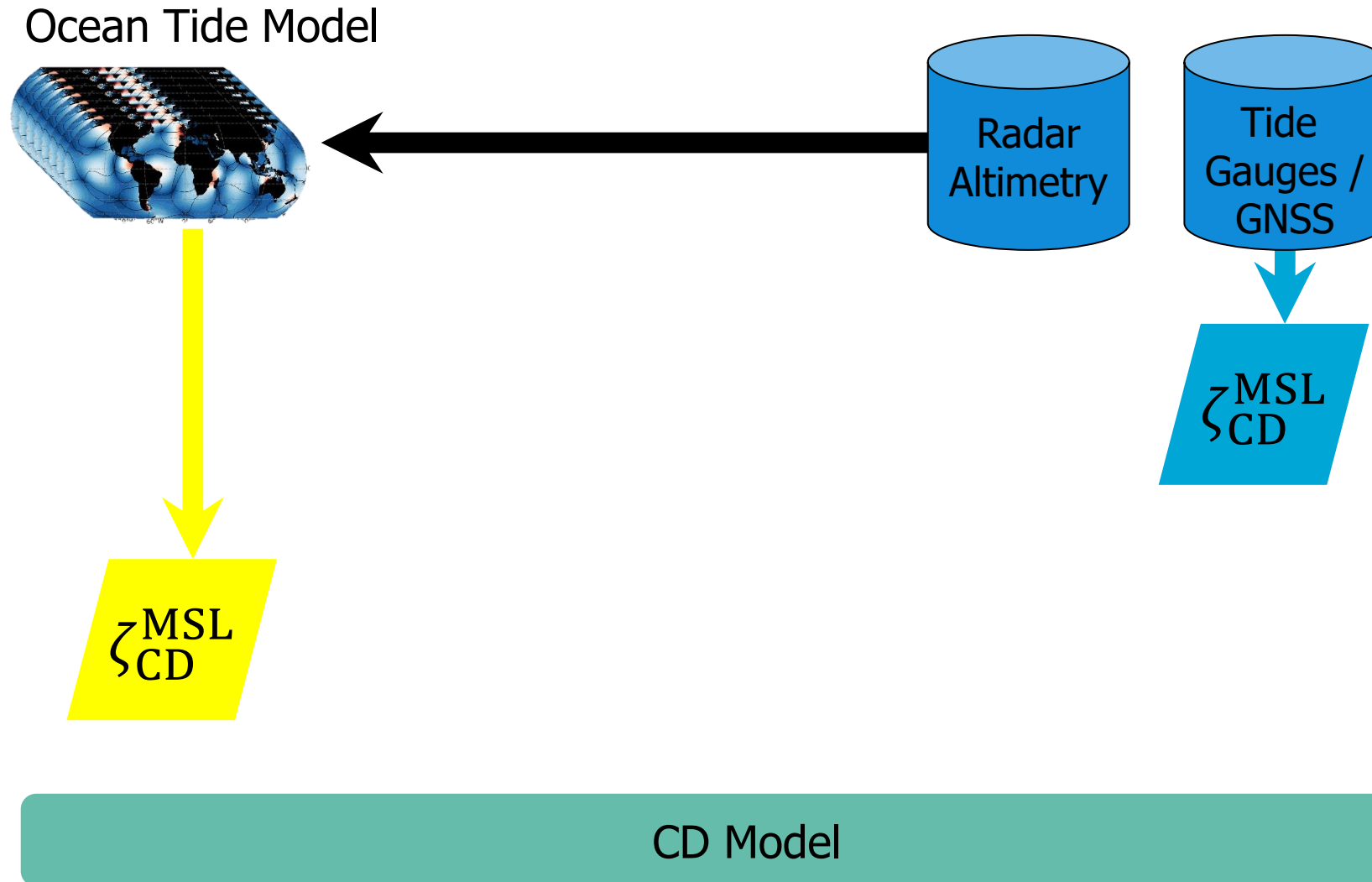
Validation in the Eastern China Marginal Seas



The 'Ocean Tide Model-Derived' CD Model



The 'Ocean Tide Model-Derived' CD Model



CONSISTENCY



in terms of...

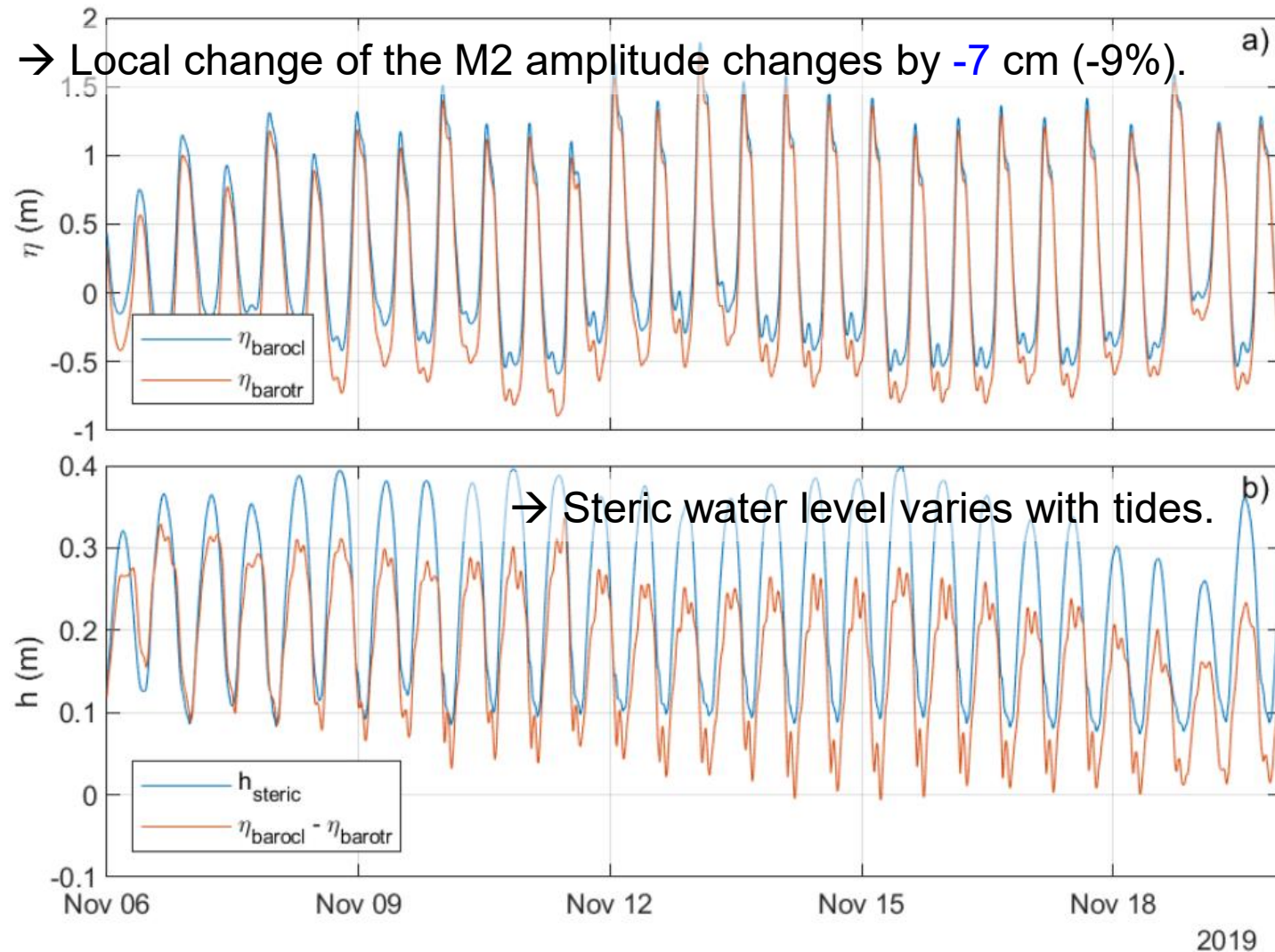
- # CONSISTENCY
1. **Analysis period** – Altimeter-derived tides are estimated from long records (1992–).
 2. **Reference epoch** – For altimeter-derived MSS model, this is the center epoch of the averaging period.
 3. **Treatment radiational (atmospheric / meteorological) tides** – These are implicitly **removed** in altimeter data processing (residual signal exist).
 4. **Treatment permanent tide** – GNSS heights refer to tide-free system, altimeter-derived heights to mean tide system.
 5. **Impact vertical land motion** – Tide gauge records need correction for vertical land motion. Doing so requires co-located GNSS.
 6. **Geodetic datums being used** – For example, altimeter-derived products often use TOPEX ellipsoid.

in terms of...

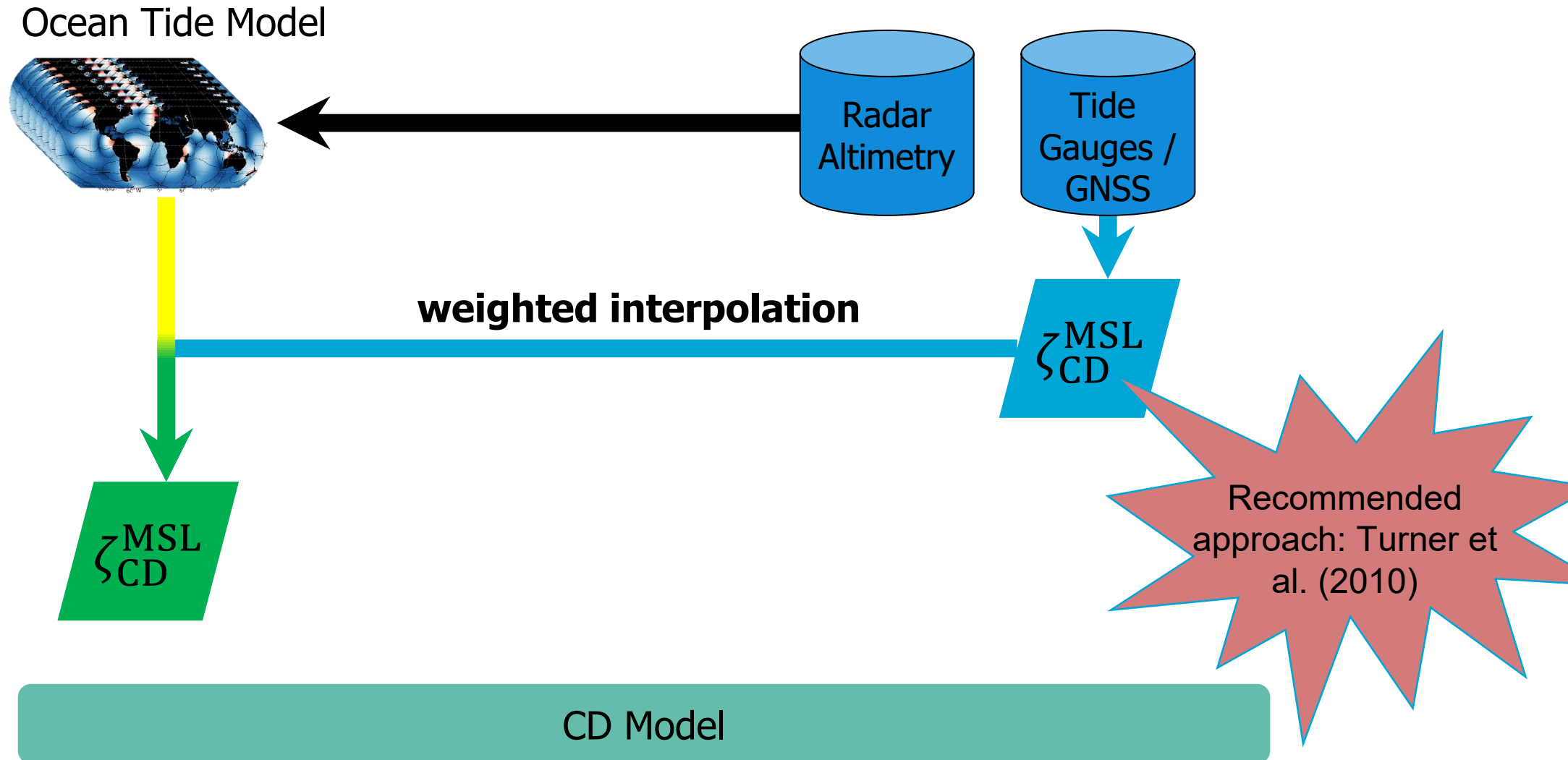
On the Use of Tide Gauges in River Mouths...



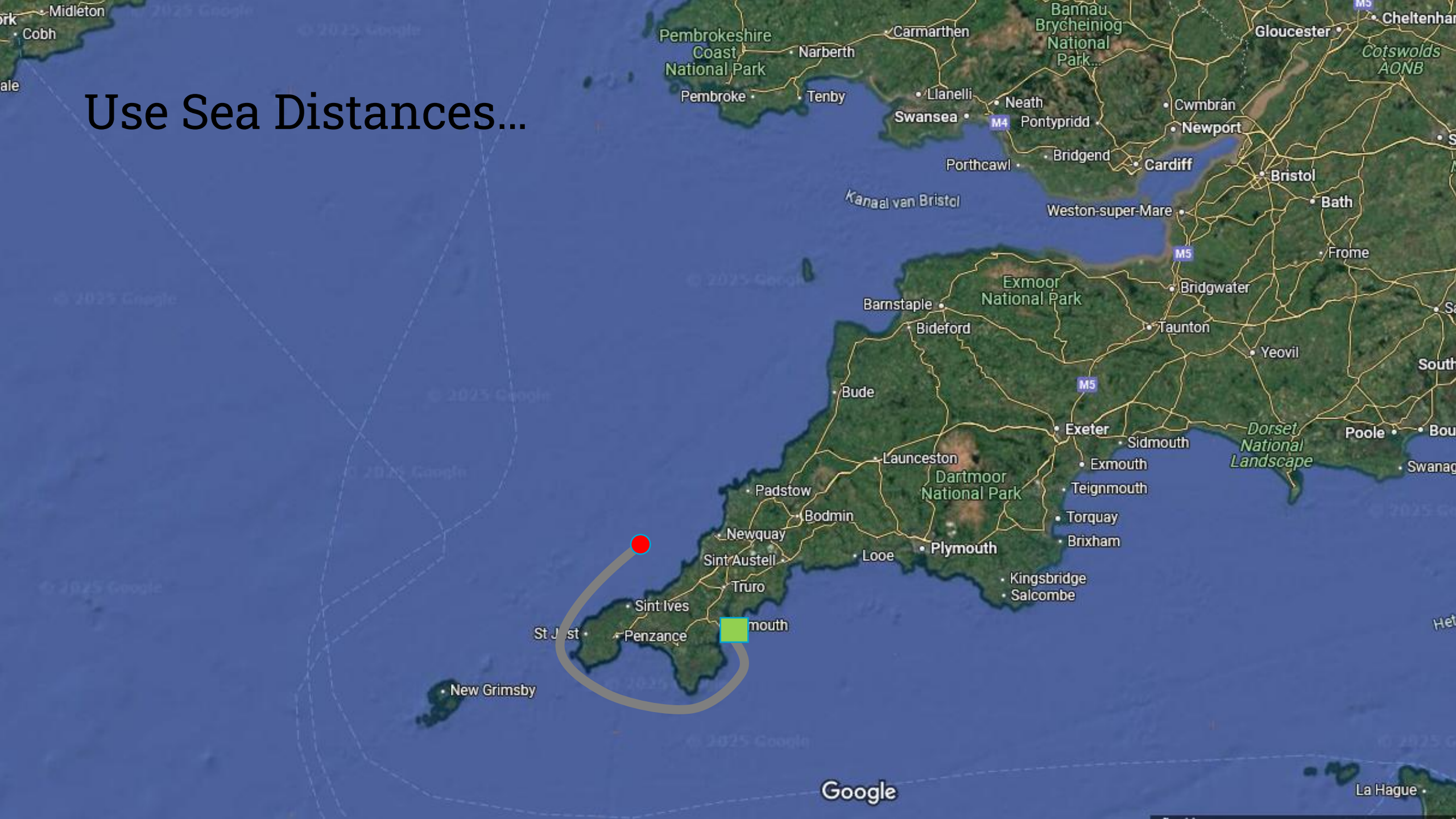
On the Use of Tide Gauges in River Mouths...



The 'Ocean Tide Model-Derived' CD Model

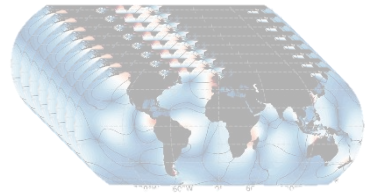


Use Sea Distances...

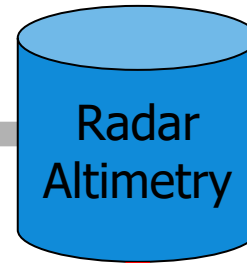


The 'Ocean Tide Model-Derived' CD Model

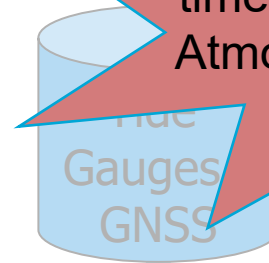
Ocean Tide Model



Radar
Altimetry



Tide
Gauges
GNSS



Note, you need to restore
time-averaged Dynamic
Atmospheric Correction!

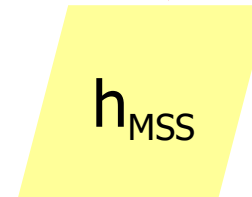
ζ_{CD}^{MSL}



ζ_{CD}^{MSL}



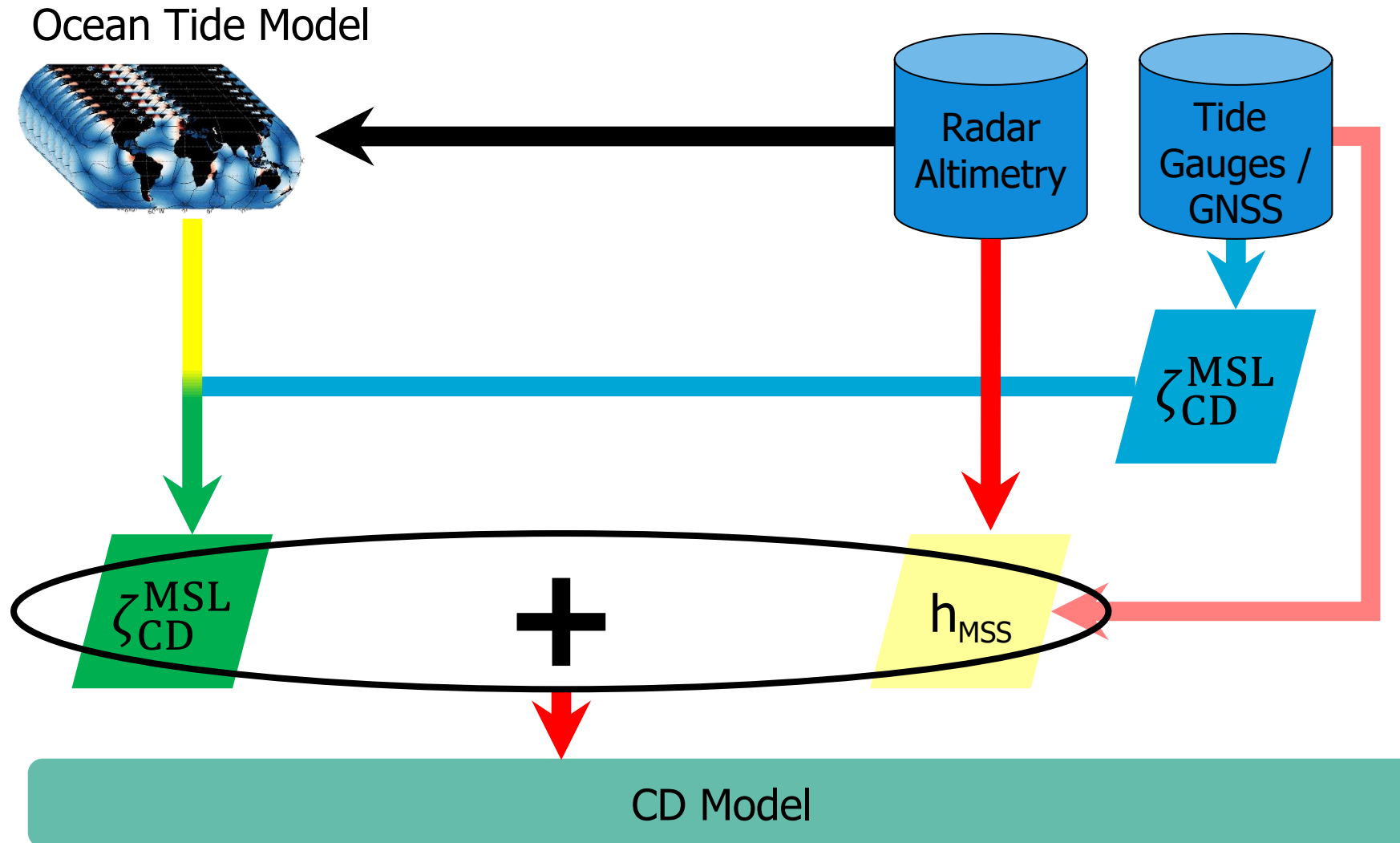
h_{MSS}



CD Model



The 'Ocean Tide Model-Derived' CD Model

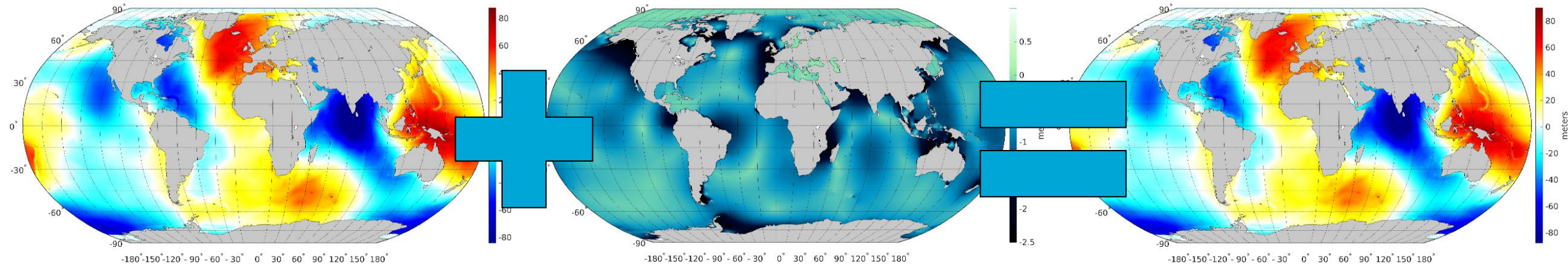


The 'Ocean Tide Model-Derived' CD Model

Global MSS model (time-averaged DAC restored)
(h_{MSS})

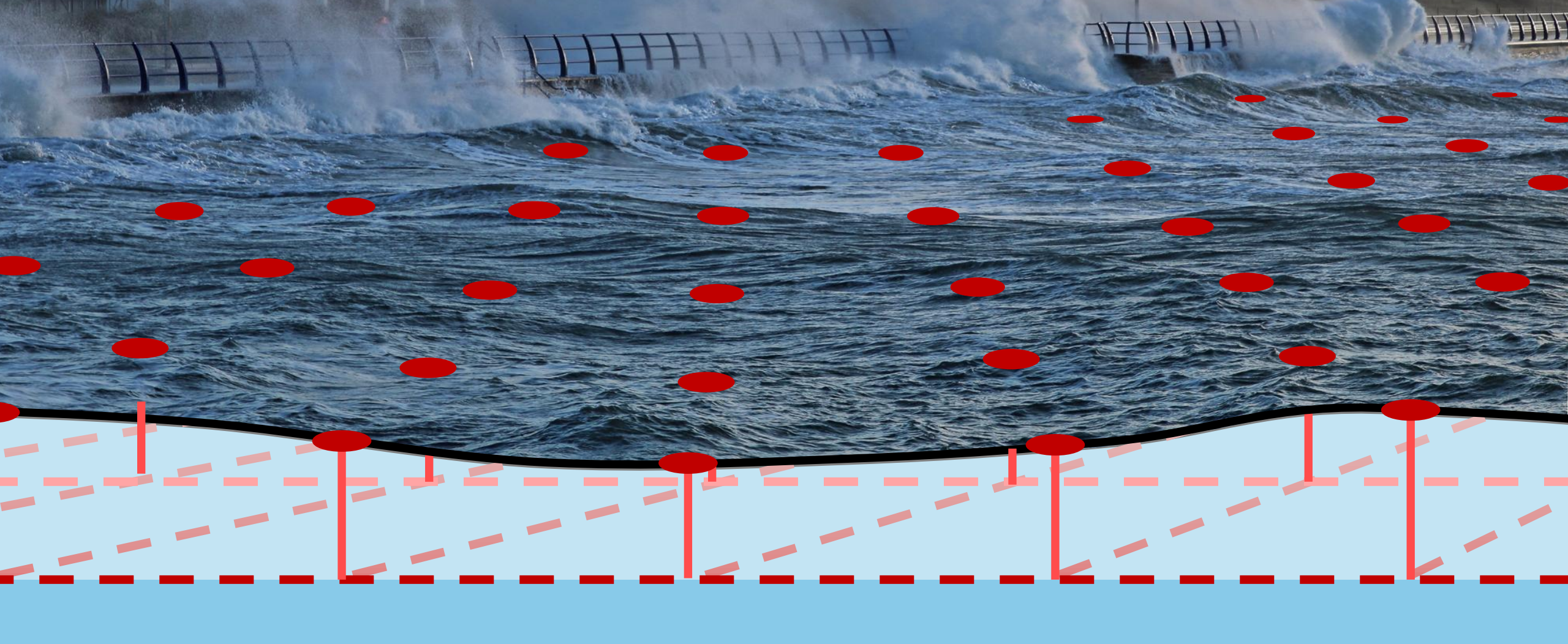
LAT w.r.t. MSL

Ellipsoidal heights of LAT
(h_{LAT})



→ Some LAT models are publicly available (e.g., DTU/CNES).

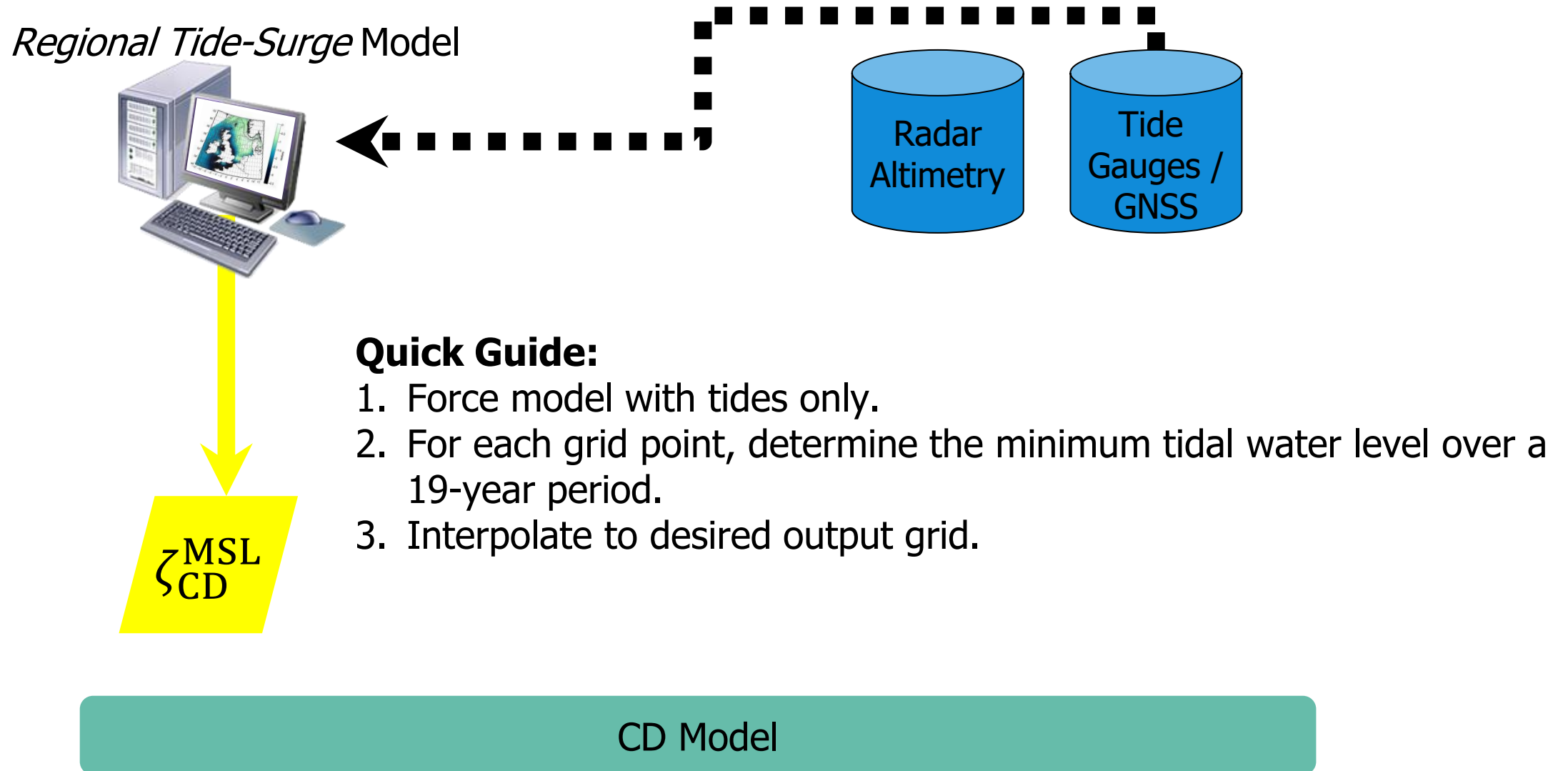
*The tidal models considered so far have all been **global** models. However, we have access to a **regional tide-surge model** that is used for storm surge predictions. How can we exploit this model for CD determination?*



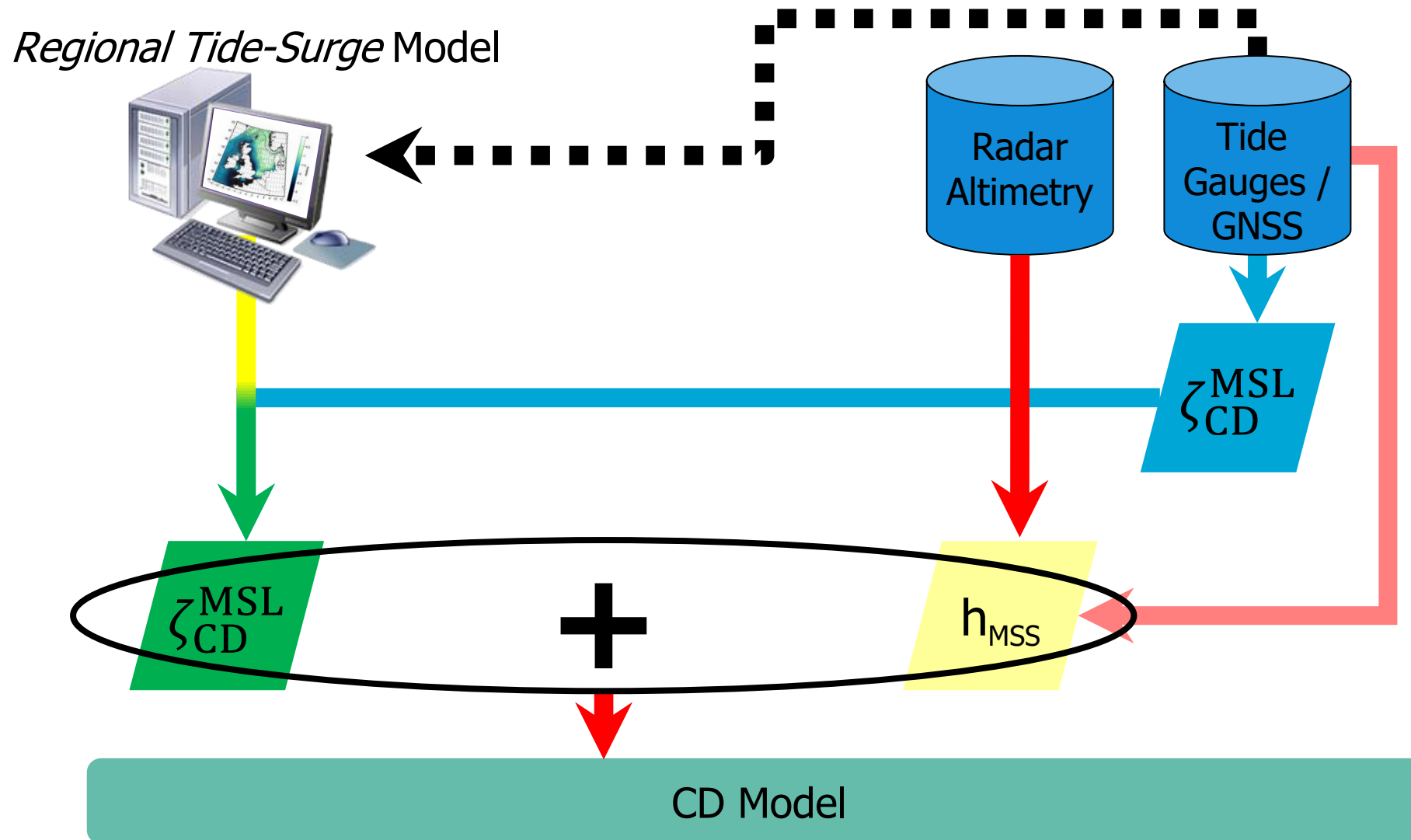
The 'Regional Tide Model-Derived' CD Model

- **Strategy:** Combine CD estimates from model-derived tidal water levels with estimates derived from tide gauges.
- Approach adopted in, e.g., the UK VORF project ([Empirical Ocean Tide model was used 30 km from the coast](#)).
- Regional models typically calibrated by tide gauge data.

The 'Regional Tide Model-Derived' CD Model



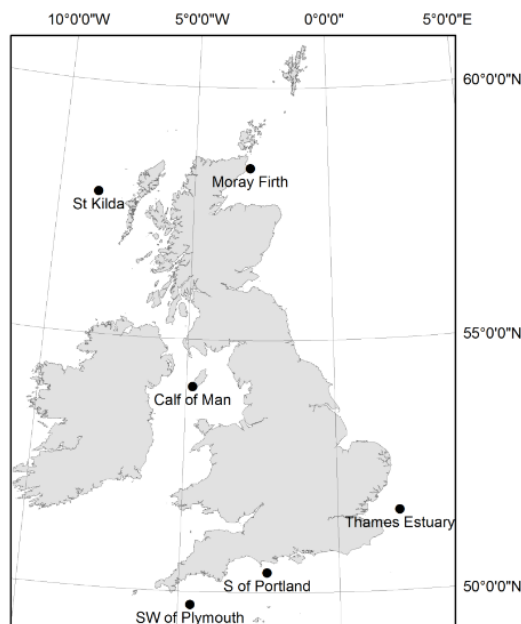
The 'Regional Tide Model-Derived' CD Model



Accuracy???

- A **non-trivial issue** due to lack of independent estimates...
- Iliffe et al. (2013): *"It is shown that across the vast majority of the domain of applicability the VORF surfaces meet their target accuracies of 0.10 m inshore and 0.15 m offshore (both 1s values) and the formal uncertainties are a fair reflection of the errors actually encountered."*

Accuracy testing



Point	Difference between observed value and VORF. (m)	Formal VORF uncertainty value. (m)	Distance offshore, measured to nearest land. (km)
Calf of Man	0.11	0.12	0.25
South West of Plymouth	0.11	0.12	45
South of Portland	0.69	0.18	20
Thames Estuary	0.23	0.14	45
Moray Firth	0.37	0.12	8
St Kilda	- 0.16	0.06	0 (or 65 km from Outer Hebrides)

This is the main independent check that was carried out with newly commissioned data – lots of internal checks, partial checks, etc.

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- Turner et al. (2010):

TABLE 1. Comparison with 392 ATT onshore gauges. A positive mean indicates that the wide-area model has greater range in LAT than the tide gauge data.

Wide-area model	Mean (m)	σ (m)
NISE10	-0.169	0.449
CSR4.0	-0.444	1.054
FES2004	-0.618	1.161
GOT00.2	-0.259	0.998
TPXO 7.0	0.013	0.749

TABLE 2. Comparison with 187 offshore gauges. A positive mean indicates that the wide-area model has a greater range in LAT than the tide gauge data.

Wide-area model	Mean (m)	σ (m)
NISE10	-0.102	0.358
CSR4.0	0.064	0.279
FES2004	-0.036	0.267
GOT00.2	0.102	0.301
TPXO 7.0	0.104	0.310

Accuracy???

- A non-trivial issue due to lack of independent estimates...
- Iliffe et al. (2013): *"It is shown that across the vast majority of the domain of applicability the VORF surface of 0.1 m offshore (both 15 values) and the formal uncertainties are a fair reflection of the errors actually encountered."*
- Turner et al. (2010):

TABLE 1. Comparison with 392 ATT onshore gauges. A positive mean indicates that the wide-area model has greater range in LAT than the tide gauge data.

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Accuracy VORF model is largely driven by tide gauge estimates...!

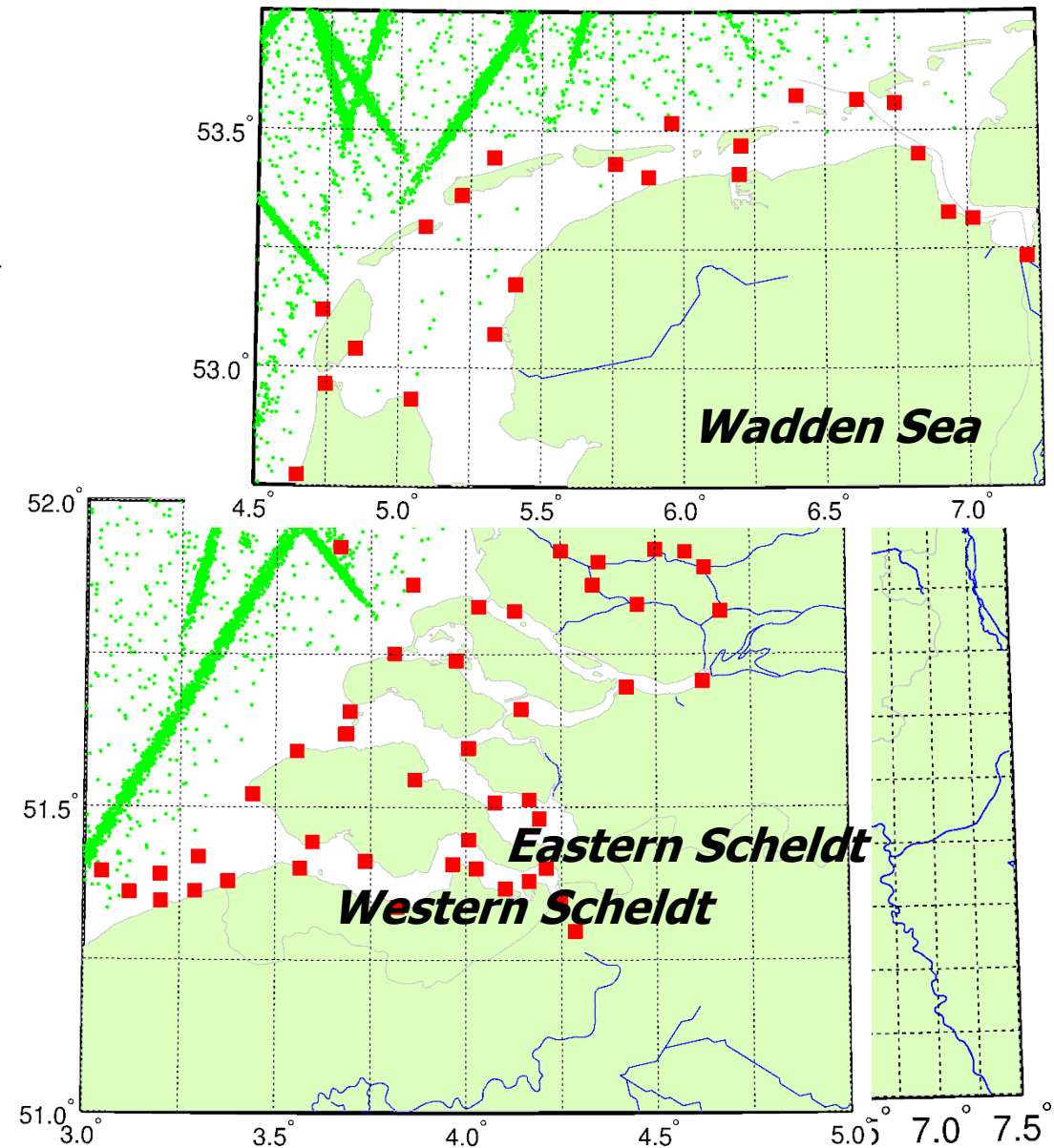
Today's models are indeed better, but...

A positive mean indicates that the wide-area model has a greater range in LAT than the tide gauge data.

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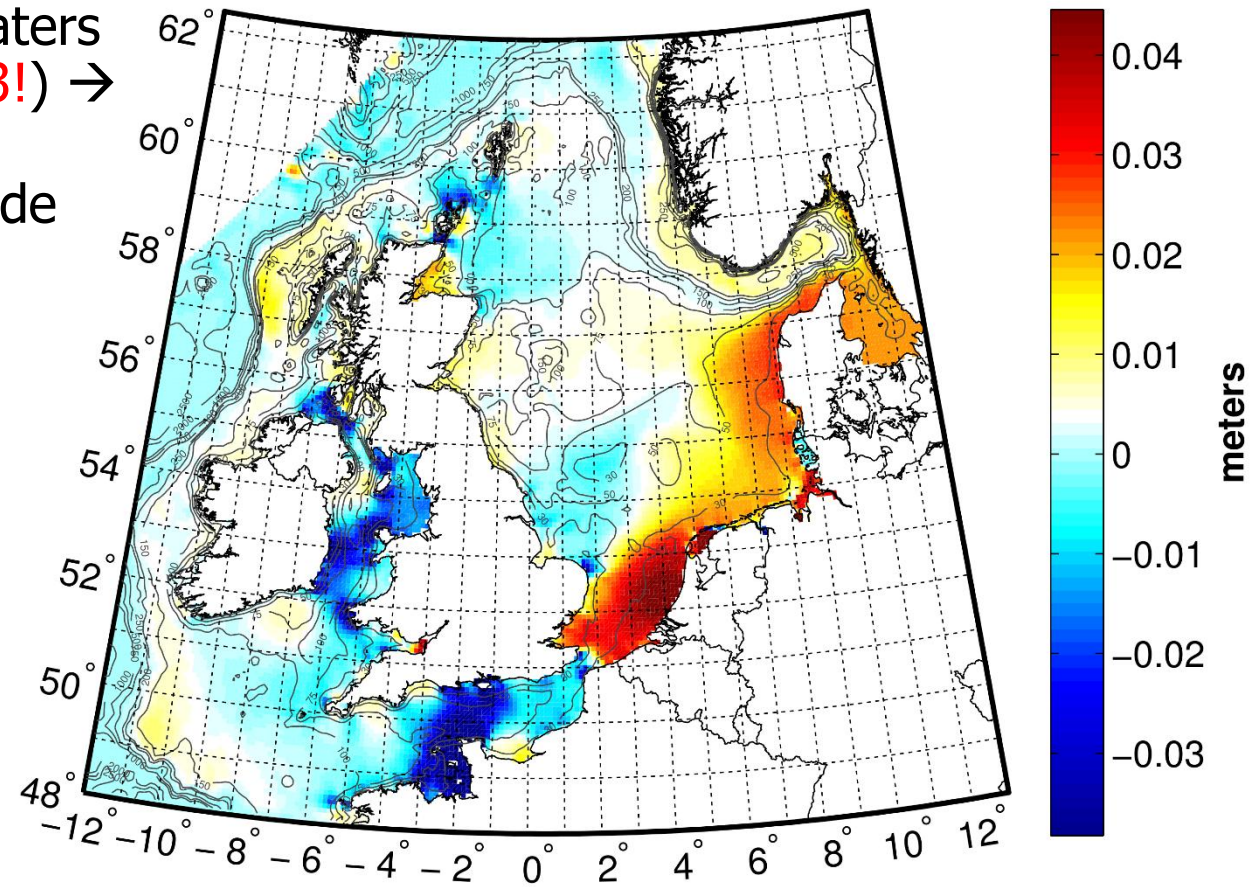
Conceptual Problems

- No reliable radar altimeter data in coastal waters + lack of tide gauges equipped with GNSS (3!) → accuracy MSS model?



Conceptual Problems

- No reliable radar altimeter data in coastal waters + lack of tide gauges equipped with GNSS (3!) → accuracy MSS model?
- MSL not the reference surface of an ocean tide model.
 - Tides contribute to MSL.
- Tide-surge interaction ignored.
- What is the MSL?
 - Thompson, JGI 63 (1980): 57-73: annual amplitudes ~ 7 cm.



Dutch Approach to Realize h_{CD} and h_{QG}

Hydro. model



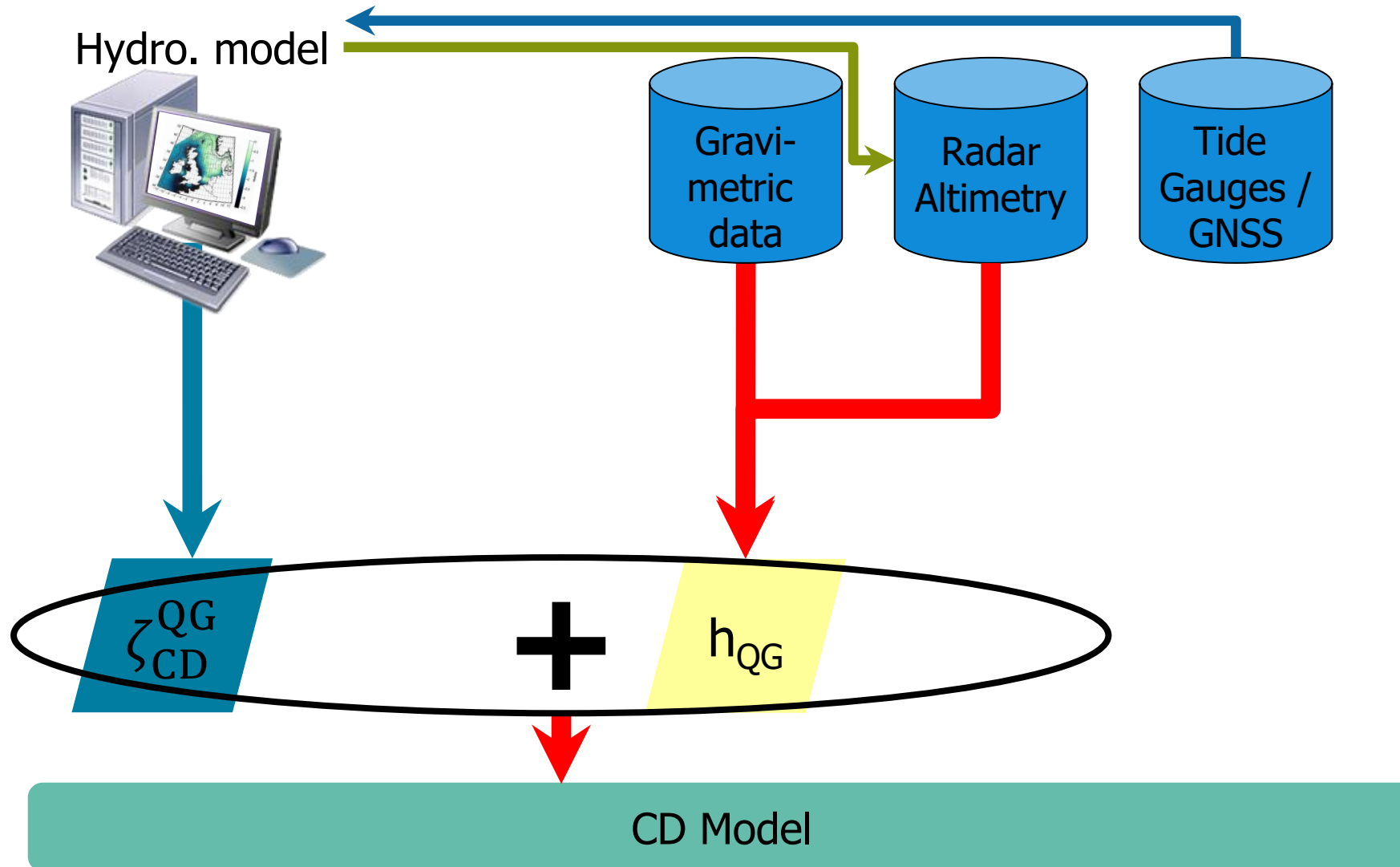
ζ_{QG}
 ζ_{CD}

Quick Guide:

1. Force model with tides + average meteo.
2. Reference model to equipotential surface adopted as ref. (Slobbe et al., 2013a).
3. For each grid point, determine the minimum tidal water level over a 19-year period.
4. Interpolate to desired output grid.

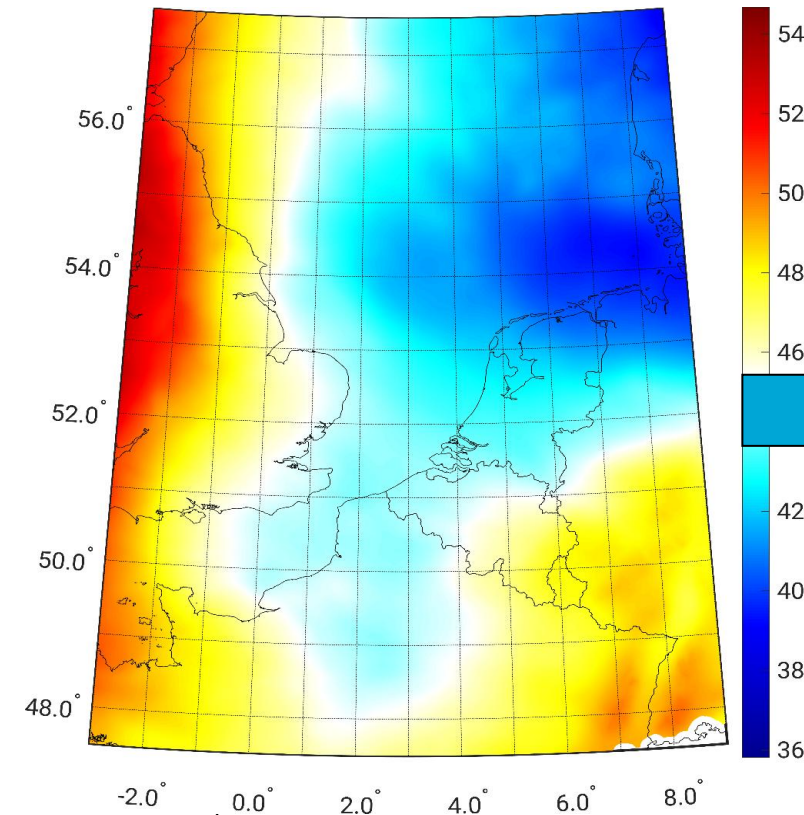
CD Model

Dutch Approach to Realize h_{CD} and h_{QG}

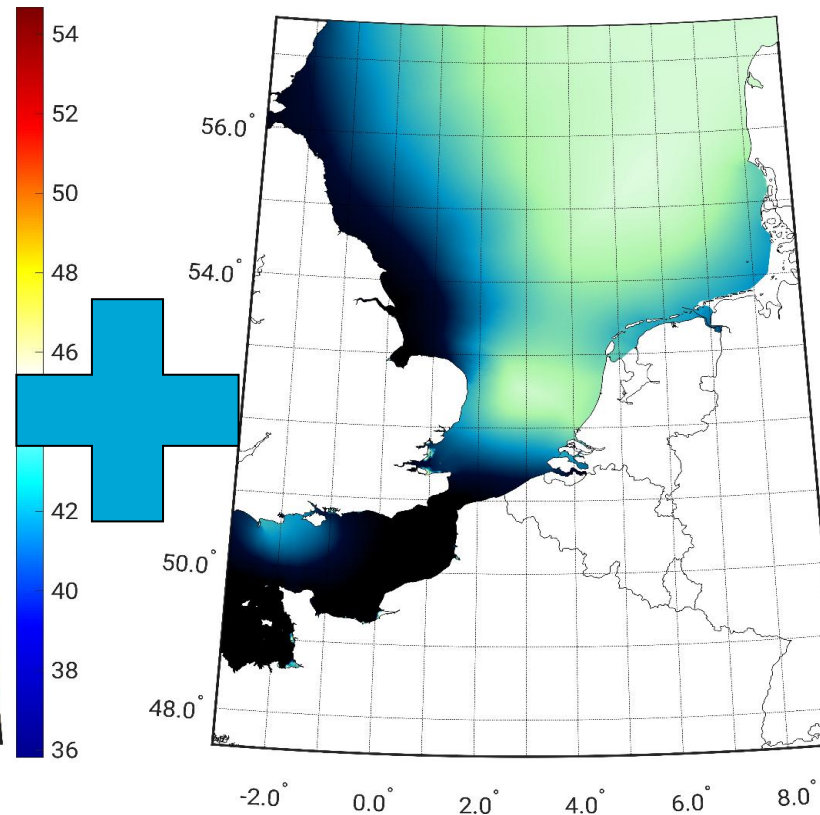


NLLAT2018

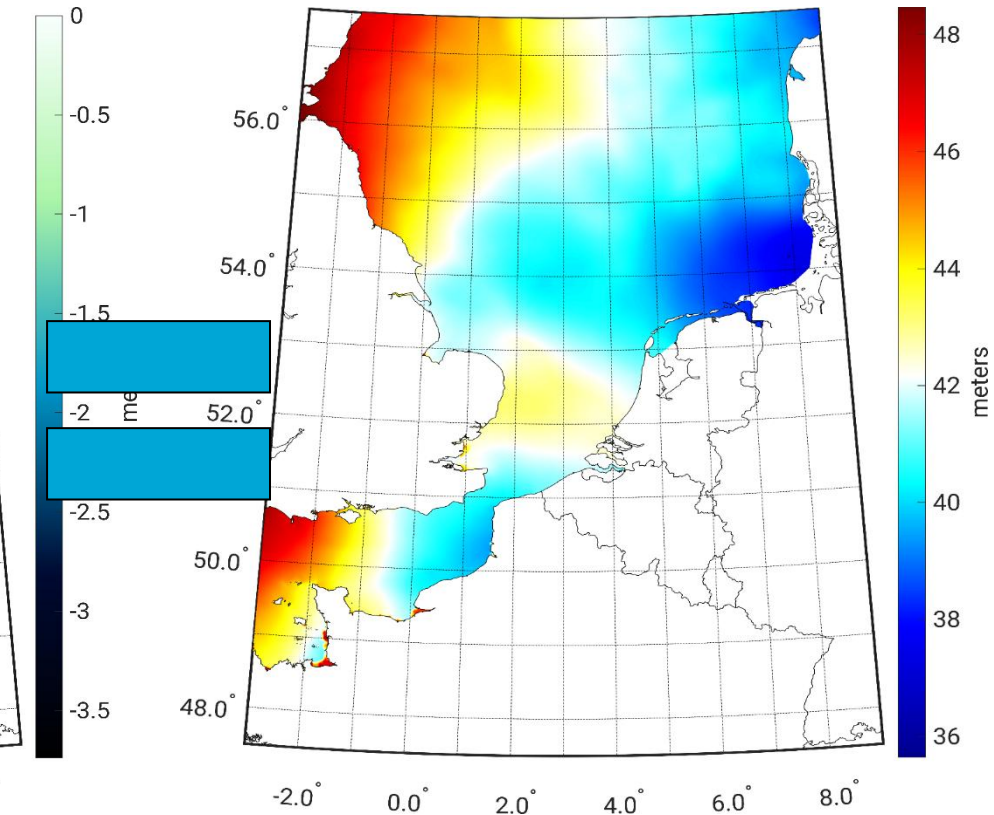
Quasi-Geoid



LAT w.r.t. Quasi-Geoid

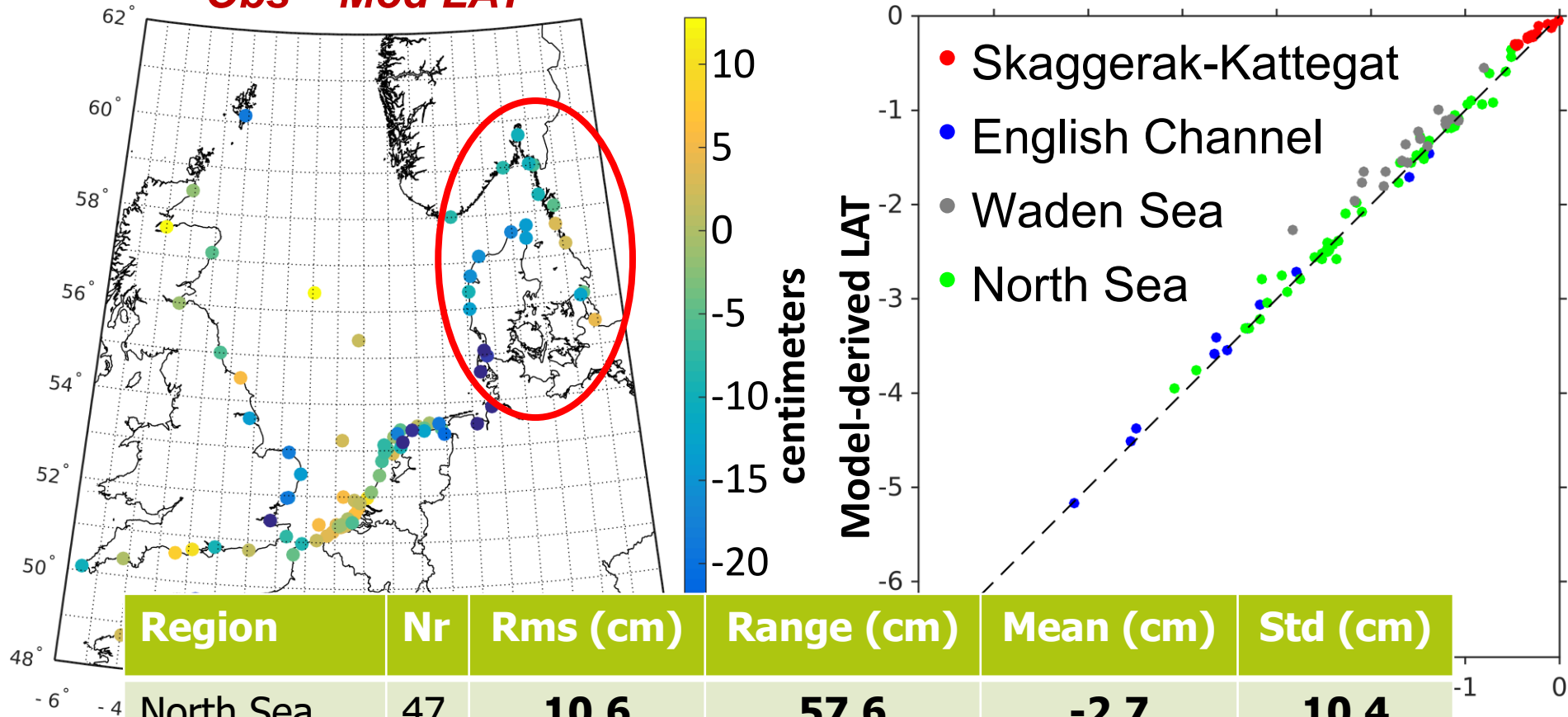


LAT w.r.t. ref. ellipsoid



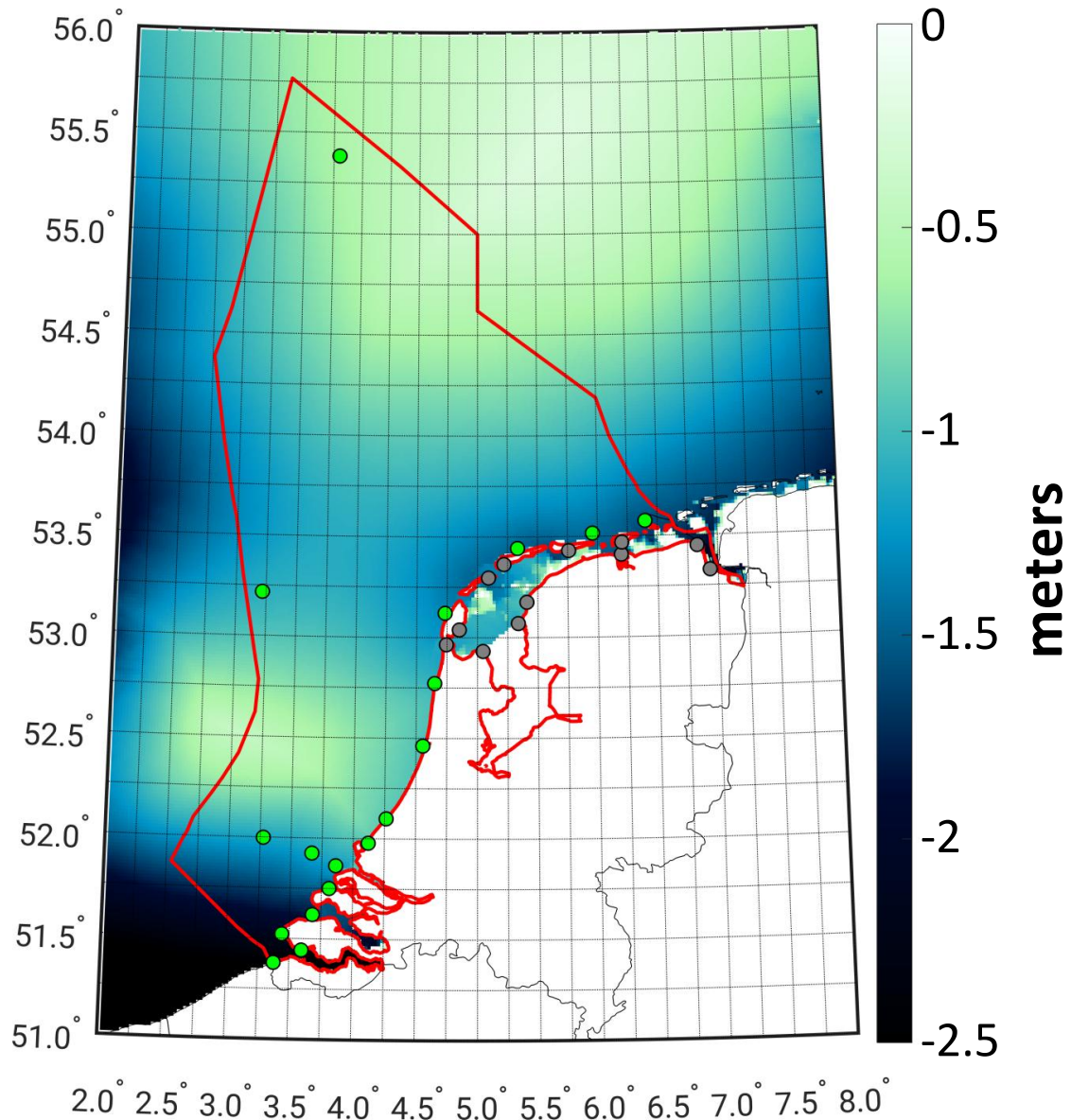
LAT w.r.t. Quasi-Geoid – Comparison

Obs – Mod LAT



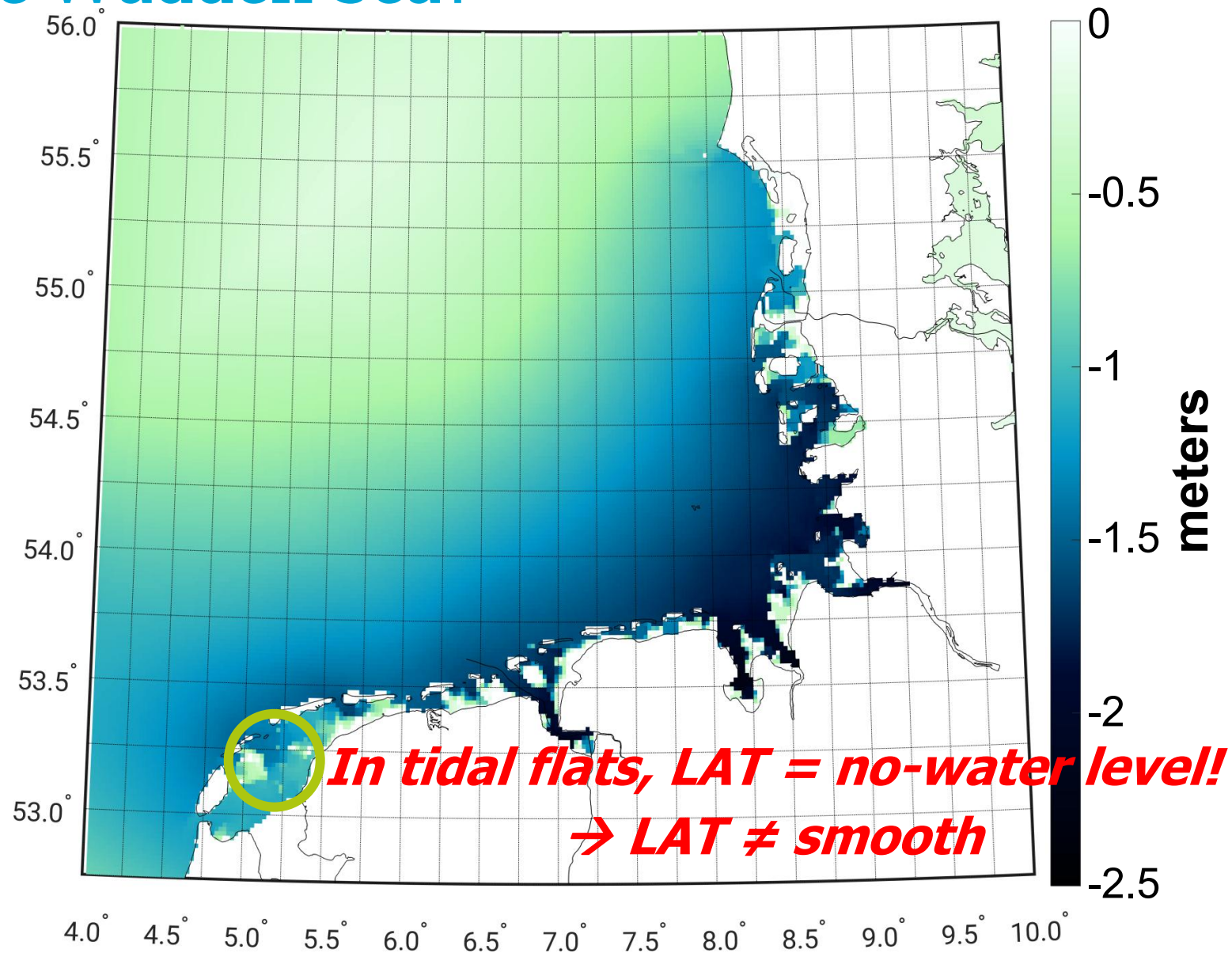
Region	Nr	Rms (cm)	Range (cm)	Mean (cm)	Std (cm)
North Sea	47	10.6	57.6	-2.7	10.4
Wadden Sea	18	24.0	59.5	-18.7	15.4
All	92	14.9	77.6	-7.2	13.1

LAT w.r.t. Quasi-Geoid –Dutch waters

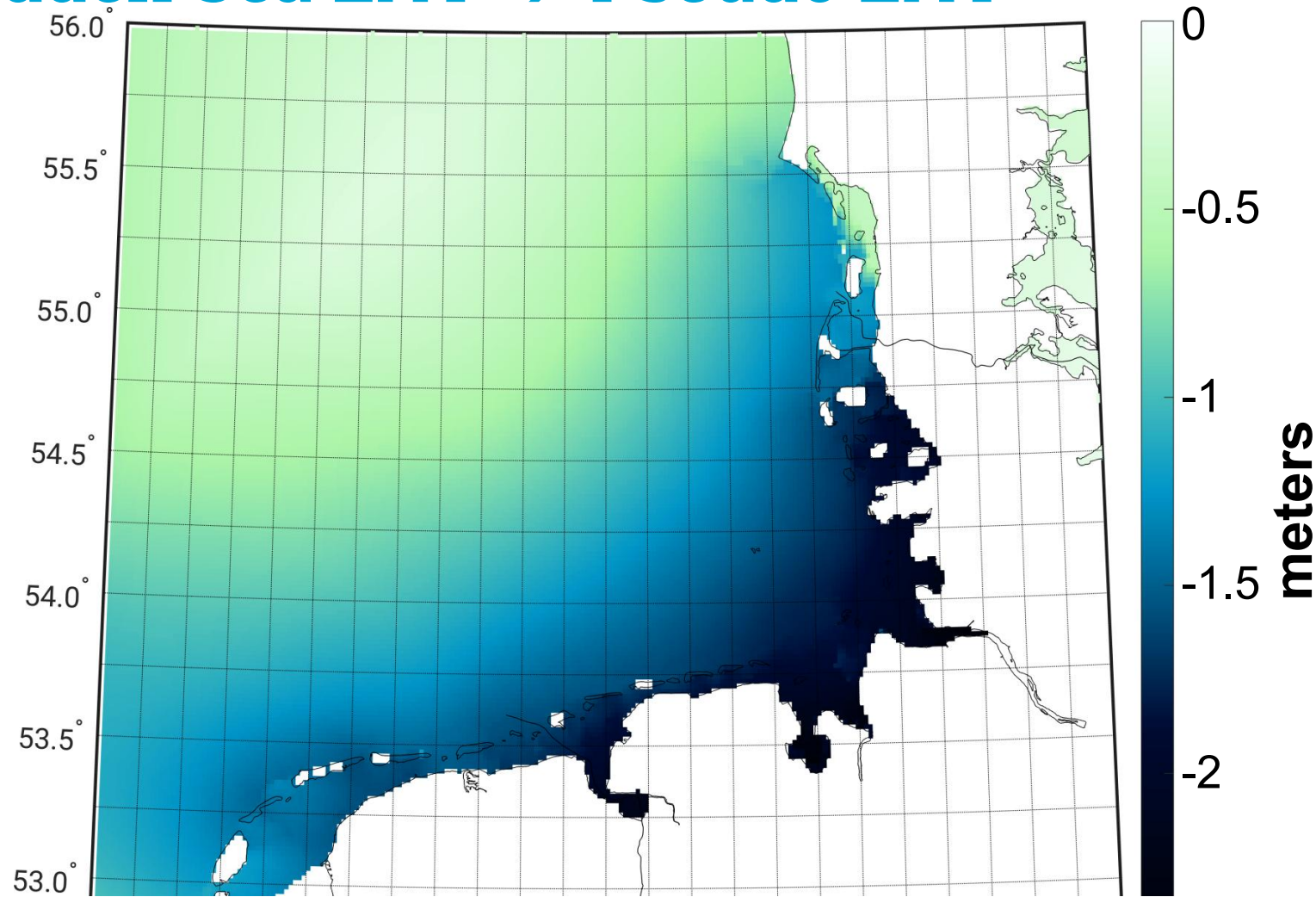


Region	Nr	rms (cm)
North Sea	19	6.6
Wadden Sea	12	14.8
All	31	10.5

LAT in the Wadden Sea?

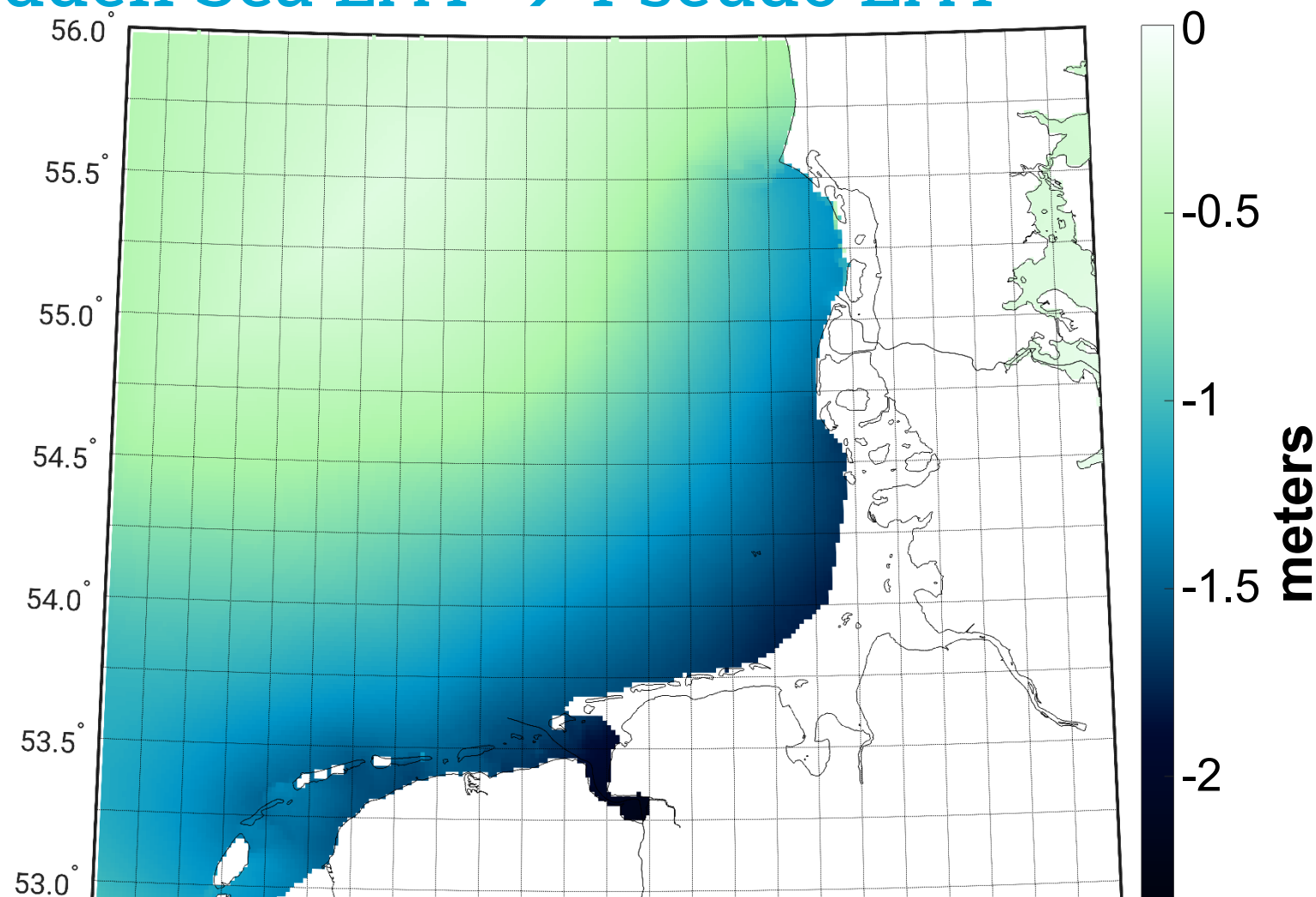


In the Wadden Sea LAT $\rightarrow$ Pseudo LAT



To obtain pseudo-LAT, we added 2 m of water to open boundary conditions & assimilated tidal water levels.

In the Wadden Sea LAT → Pseudo LAT



NOT valid outside Dutch waters!!!

A Fair Question...

*Why you didn't use
altimeter-derived tides?*



The Accuracy of Altimeter-Derived Tides...

"For the combined eight major tidal constituents, the root sum of squares is 0.89, 5.1, and 6.5 cm for pelagic, shelf, and coastal conditions, respectively." (Stammer et al., 2014)

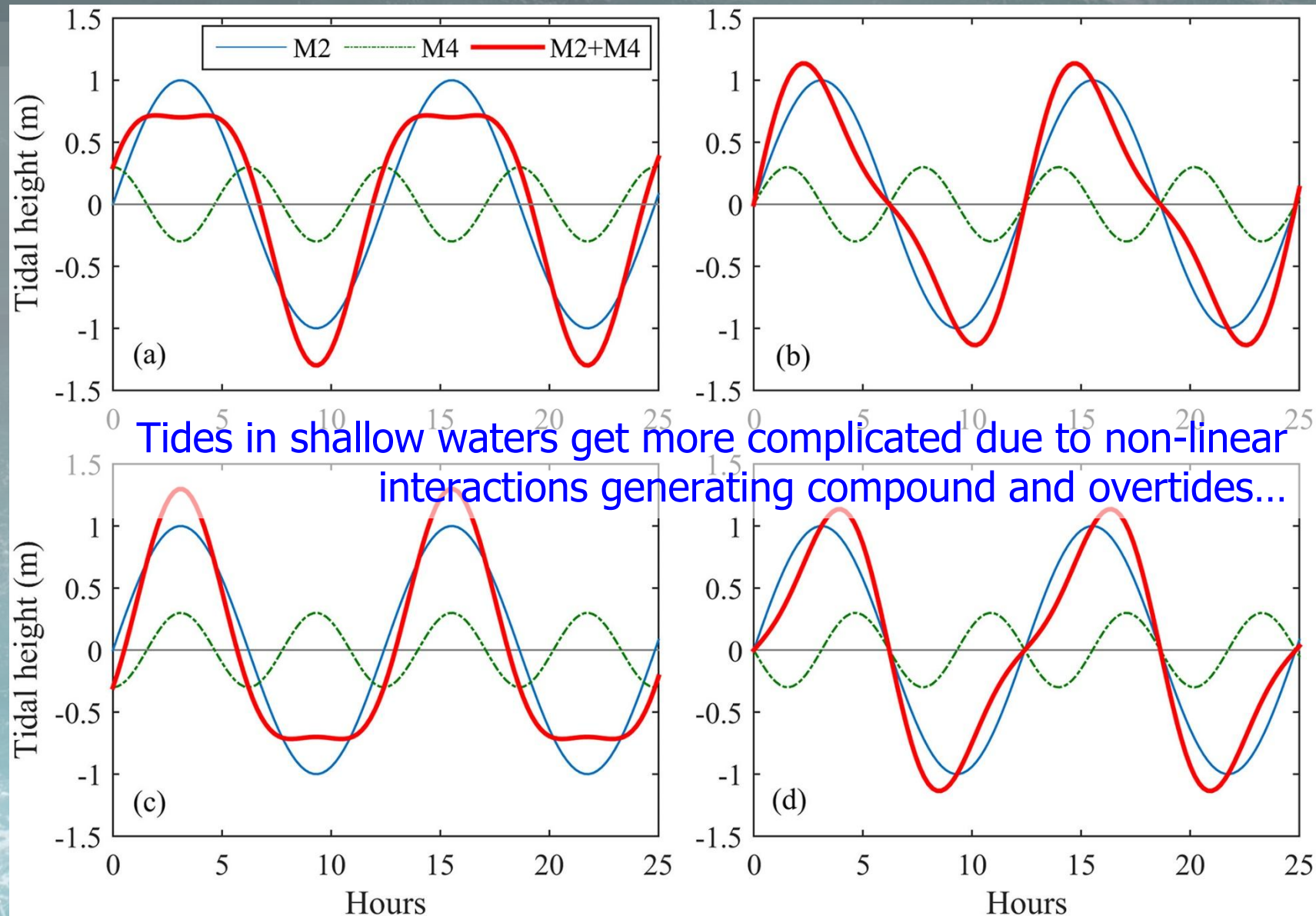
The Accuracy of Altimeter-derived tides...

Gregg, D. E., Penna, N. T., Jones, C., & Maqueda, M. A. M. (2024). Accuracy assessment of recent global ocean tide models in coastal waters of the [European North West Shelf](#). Ocean Modelling, 192, 102448.

Table 4

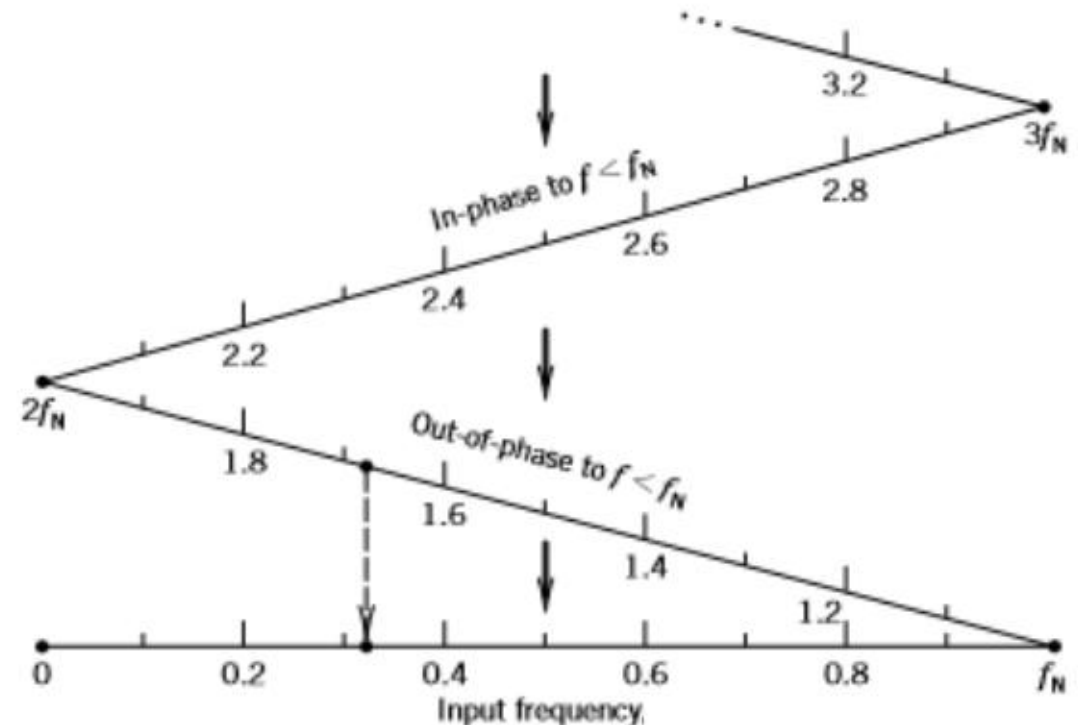
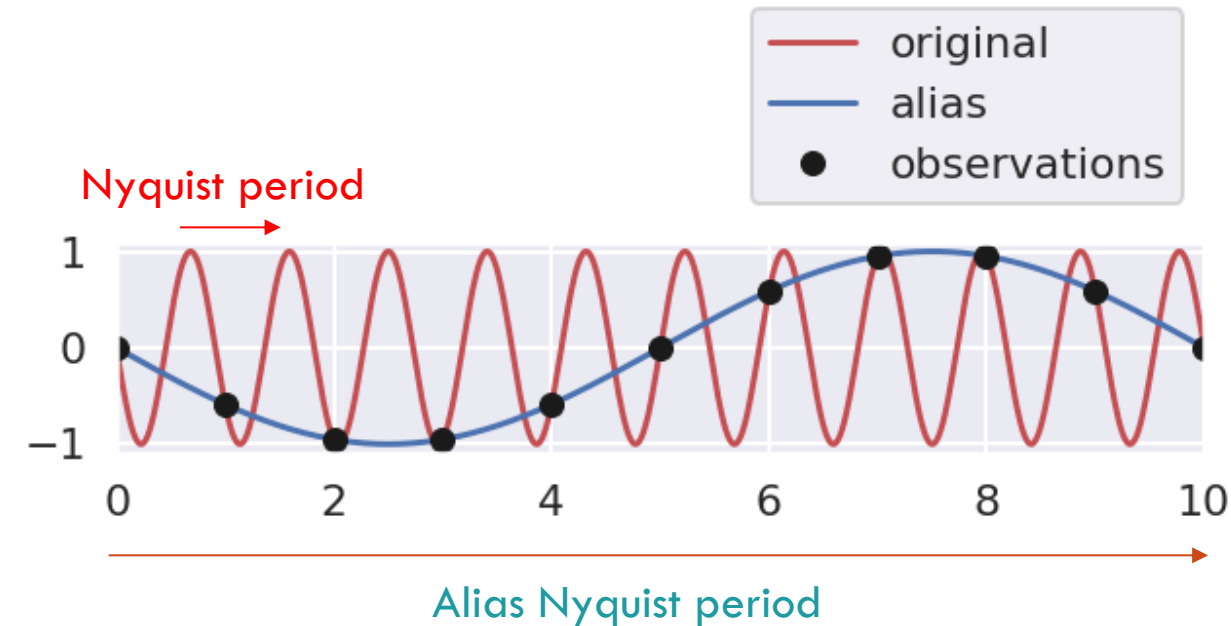
RSS (cm) across eight constituents (M2, S2, N2, O1, K1, K2, P1, and Q1) of three different statistical measures summarising the phasor residuals between model predictions and the observed values at 137 TG and BPR considered to be independent (not assimilated by the global tide models). It is displayed overall, as well as split into various zones defined by ocean depth. Bold indicates the best performance.

	FES2014b	EOT20	DTU16	TPX09
<i>RMS</i>				
Coastline	24.46	25.50	33.22	42.37
Coastal	8.70	8.69	8.98	8.61
Shelf	4.62	4.70	4.68	4.89
Ocean	3.21	3.38	3.57	3.16
Overall	16.47	17.07	21.66	27.09
<i>MAR</i>				
Coastline	12.28	14.65	15.95	15.31
Coastal	4.77	4.77	5.02	5.33
Shelf	2.62	2.96	2.48	2.86
Ocean	3.16	3.22	3.34	3.01
Overall	5.61	5.56	5.35	5.89
<i>Voronoi-weighted RMS (×10⁻²)</i>				
Coastline	9.74	10.09	12.92	11.39
Coastal	6.52	6.67	6.69	6.73
Shelf	7.02	7.17	7.13	7.40
Ocean	5.12	5.39	5.69	5.03
Overall	7.93	8.17	9.60	8.84



Tides in shallow waters get more complicated due to non-linear interactions generating compound and overtides...

Limitations due to poor altimeter sampling...

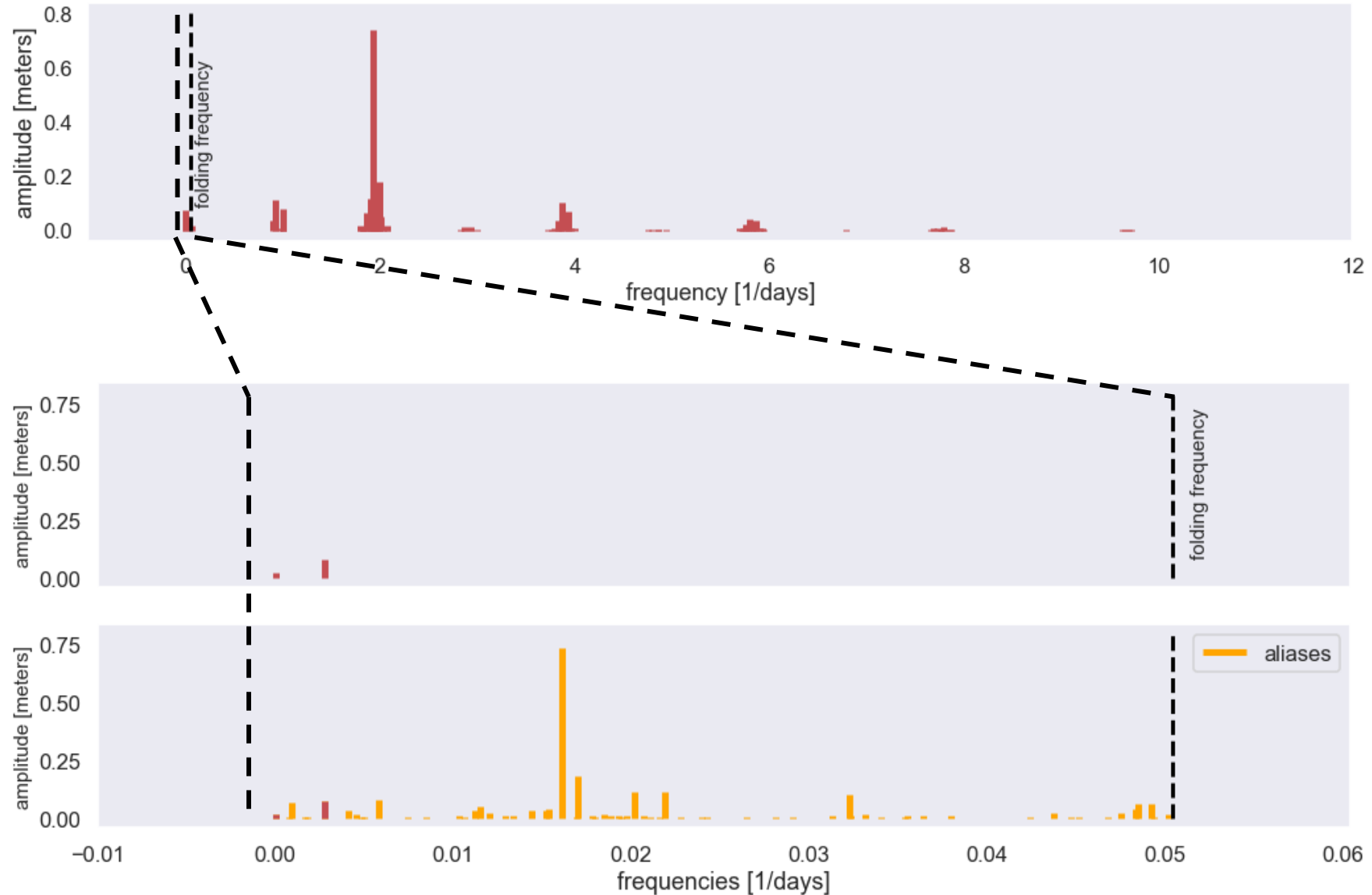


Example: Offshore Tide Gauge – North Sea

All of the frequencies right of the Nyquist (folding) frequency get folded into a new perceived frequency in between it and zero

before folding...

... and after folding

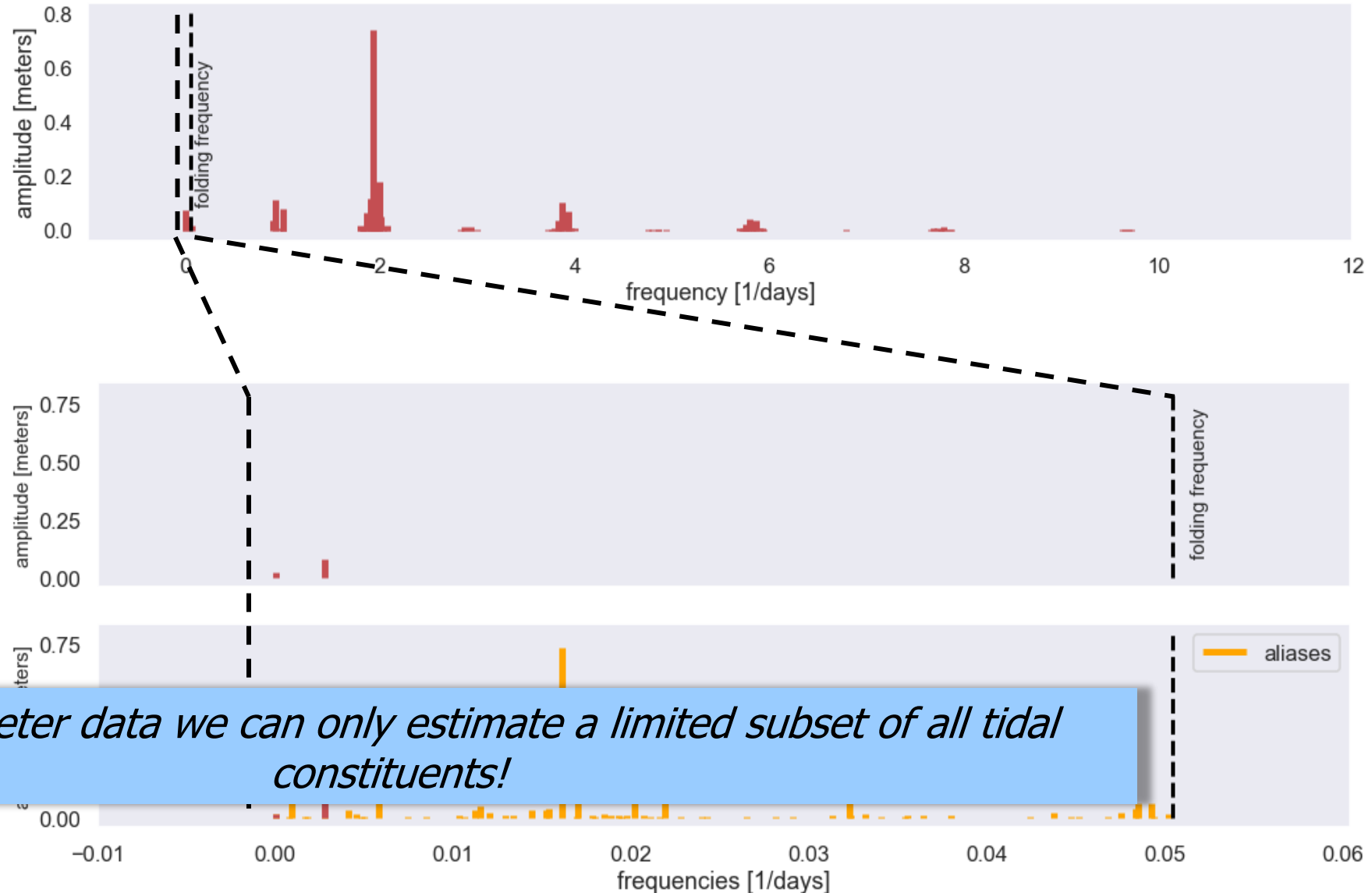


Example: Offshore Tide Gauge – North Sea

All of the frequencies right of the Nyquist (folding) frequency get folded into a new perceived frequency in between it and zero

before folding...

... and c



Based on altimeter data we can only estimate a limited subset of all tidal constituents!

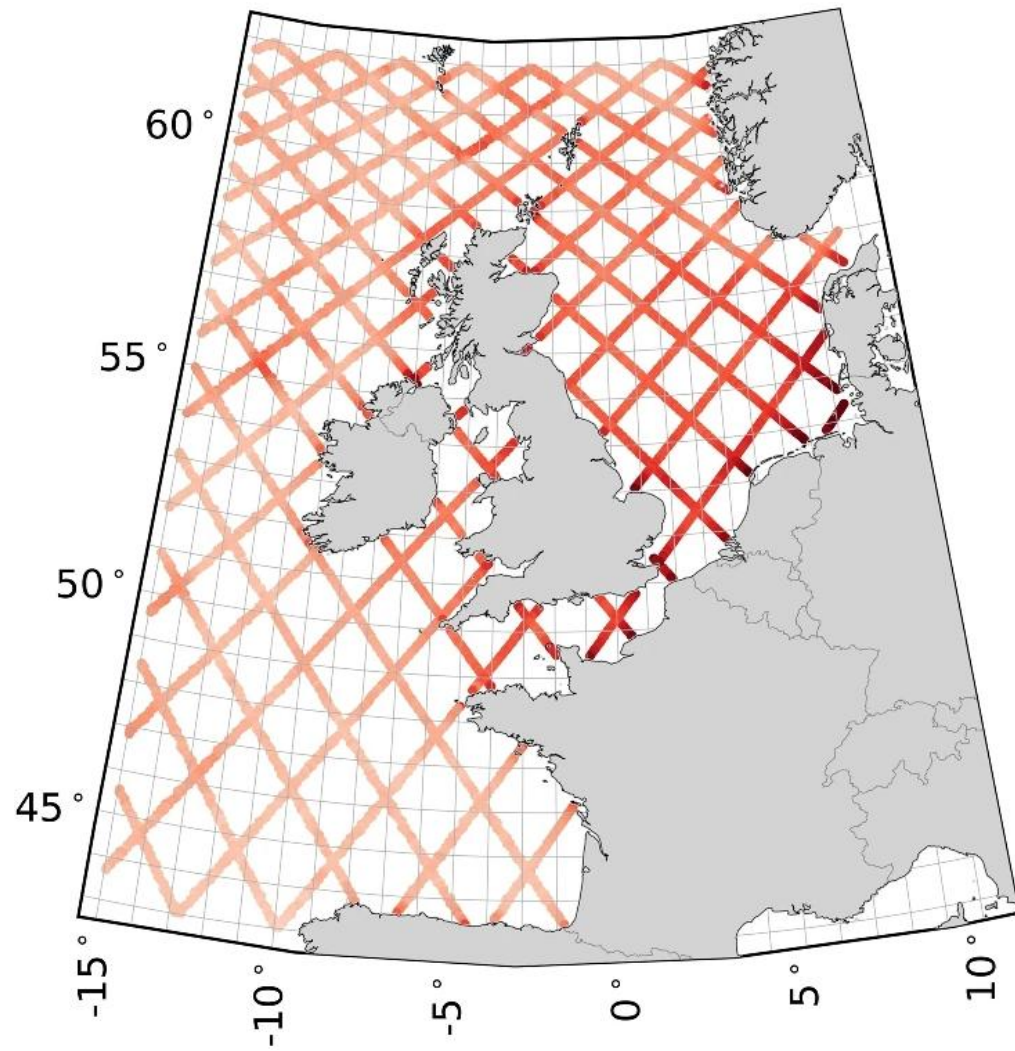
Tide-Surge Interactions Ignored...

Nonlinear tide-surge interactions alter the *phase* of tidal signals while the *tides themselves modulate non-tidal signals*. They are reported in numerous locations globally...

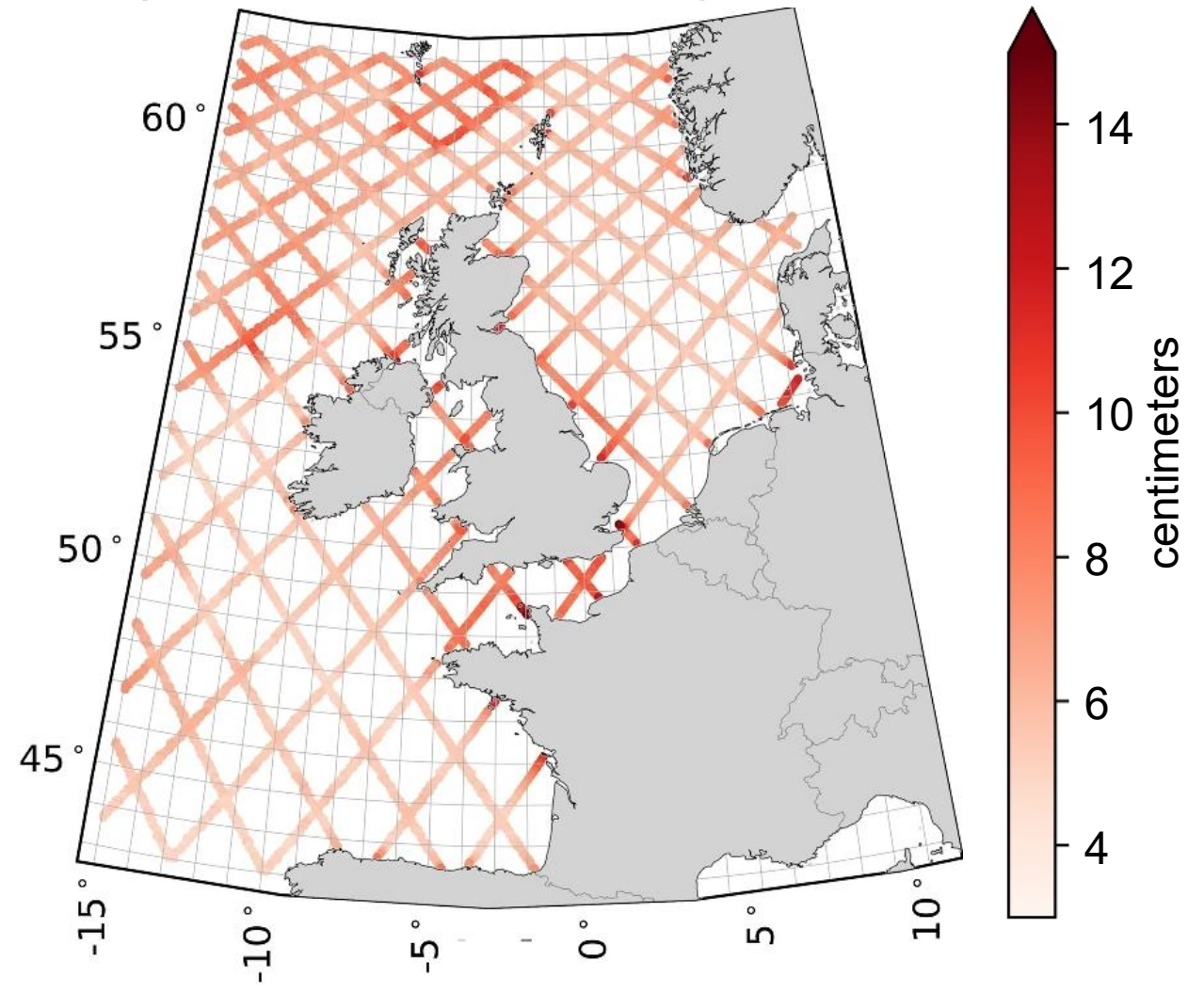
Total water level $\neq$ Tides + Surge + ...

SD residual water level time series obtained by applying:

**FES2022b tide + DAC surge corrections
(excl. nonlinear tide-surge interactions)**



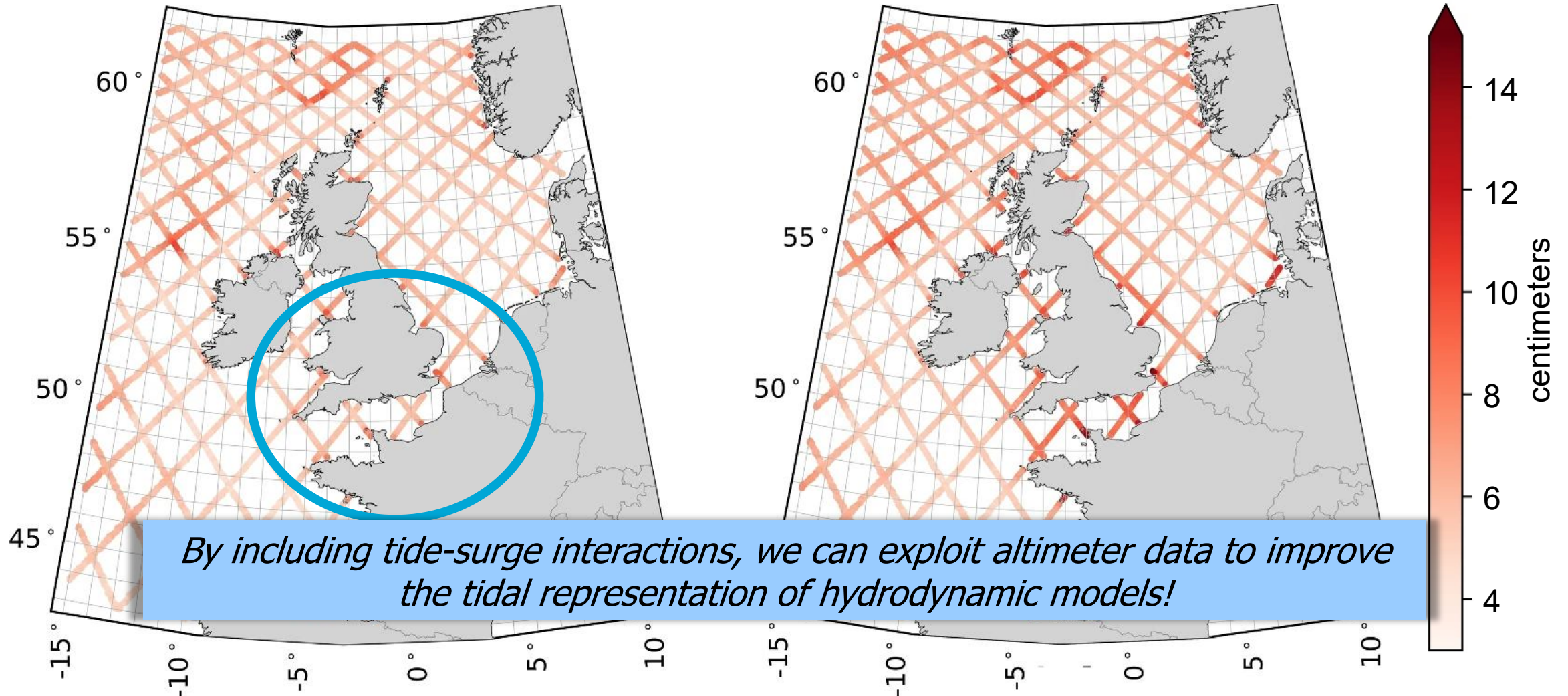
**DCSM-derived tide-surge corrections
(incl. nonlinear tide-surge interactions)**



Key to Improve Tidal Representation in Hydr. Models!

DCSM-derived tide-surge corrections
+ residual tide correction

DCSM-derived tide-surge corrections
(including nonlinear tide-surge interactions)



If our **HydroLev** Research Proposal Will be Granted...



Rijkswaterstaat
Ministry of Infrastructure and the
Environment



Royal Netherlands Navy

GEODELTA

Deltares



TUS

Ollscoil Teicneolaíochta na Sionainne:
Lár Tíre, An tIarthar Láir
Technological University of the Shannon:
Midlands Midwest

NGI
Nationaal
Geografisch
Instituut



IGN
Institut
Géographique
National



Boskalis

**TAL
TECH**



TU Delft

Delft
University of
Technology

TUM



JAN DE NUL



DEME



ARISTOTLE
UNIVERSITY
OF THESSALONIKI



Bundesamt für
Kartographie und Geodäsie

Van Oord

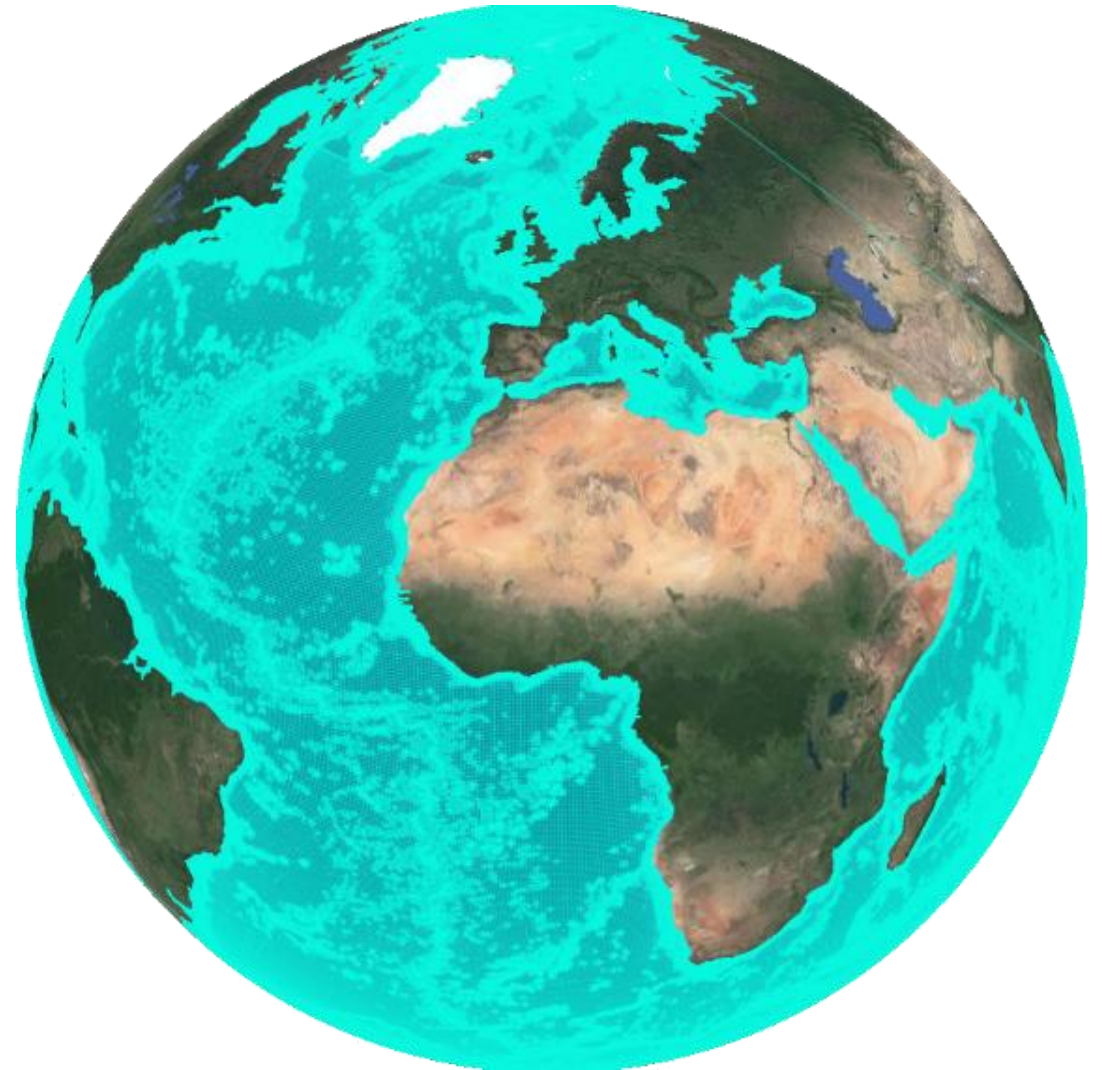


Marine ingenuity

FUGRO

We Will...

- Apply the approach by Guarneri et al. (2025) to compute an **altimeter-derived along-track tidal product** for the global oceans $< 66^\circ$ latitude.
- Use the product to calibrate the **Global Tide and Surge Model**.
- Compute a **global** CD model from **water level time series** obtained with the recalibrated GTSM Model assimilated with tide gauge water levels and a MSS model.



The Recommended Approach...?

- Begin with a simple approach.
- Be pragmatic.
- The main challenge lies in maintaining consistency among chart datum values derived from different sources.
- Rather than reinventing the wheel, align with established methodologies.
- If you like to discuss, feel free to contact me (D.C.Slobbe@tudelft.nl)